



Coimisiún na Scrúduithe Stáit
State Examinations Commission

Junior Certificate Examination, 2012

Mathematics
(Project Maths – Phase 2)

Paper 1

Higher Level

Friday 8 June Afternoon 2:00 to 4:30
300 marks

Examination number

Centre stamp

Running total	
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For examiner			
Question	Mark	Question	Mark
1		11	
2		12	
3		13	
4		14	
5			
6			
7			
8			
9			
10		Total	

Grade

Instructions

There are 14 questions on this examination paper. Answer **all** questions.

Questions do not necessarily carry equal marks. To help you manage your time during this examination, a maximum time for each question is suggested. If you remain within these times you should have about 10 minutes left to review your work.

Question 14 carries a total of 50 marks.

Write your answers in the spaces provided in this booklet. There is space for extra work at the back of the booklet. You may also ask the superintendent for more paper. Label any extra work clearly with the question number and part.

The superintendent will give you a copy of the booklet of *Formulae and Tables*. You must return it at the end of the examination. You are not allowed to bring your own copy into the examination.

Marks will be lost if all necessary work is not clearly shown.

Answers should include the appropriate units of measurement, where relevant.

Answers should be given in simplest form, where relevant.

Write the make and model of your calculator(s) here:

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Question 1 (Suggested maximum time: 5 minutes)

Question 1 (Suggested maximum time: 5 minutes)

- (a)** Give two reasons why -7.3 is not a natural number.

Reason 1:

Reason 2:

[illegible]

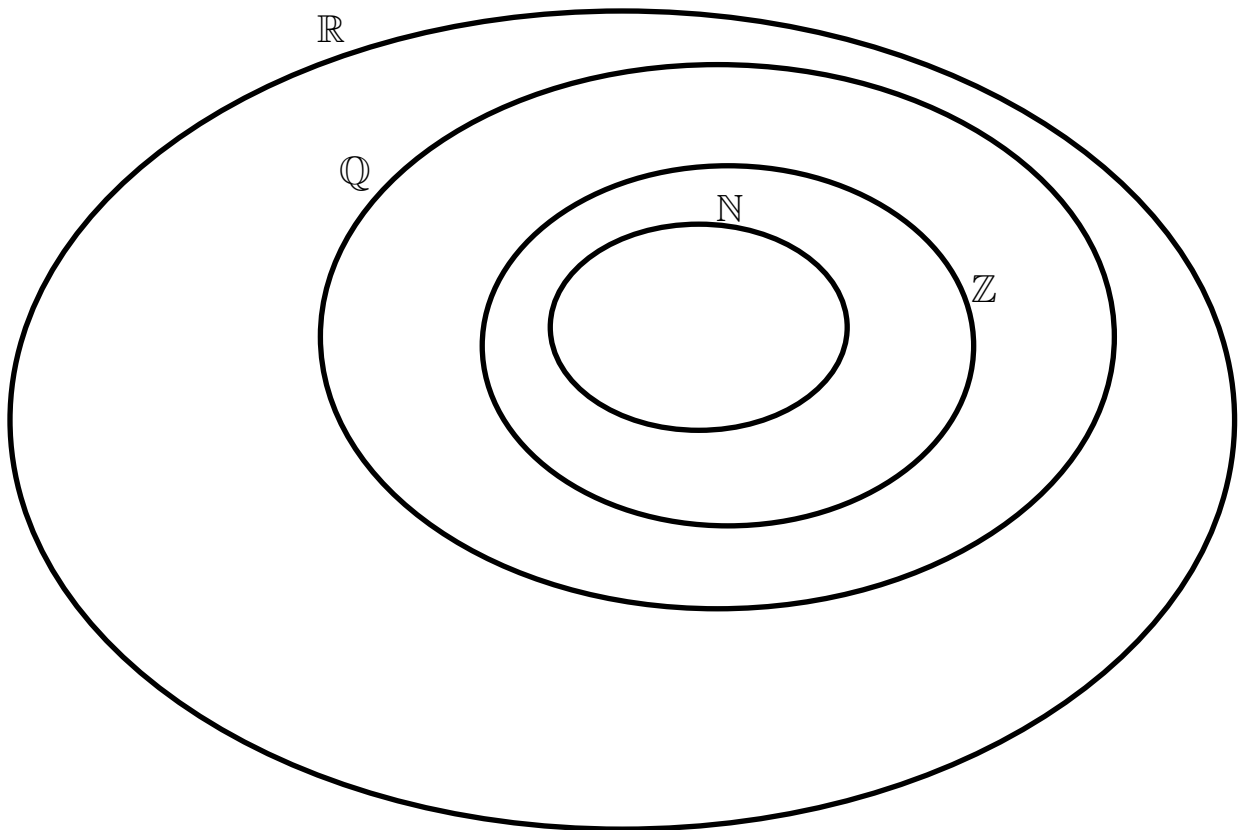
- (b)** The diagram represents the sets:

Natural Numbers $\mathbb{N}$

Integers $\mathbb{Z}$

Rational Numbers $\mathbb{Q}$

Real Numbers $\mathbb{R}$



Insert each of the following numbers in the correct place on the diagram:

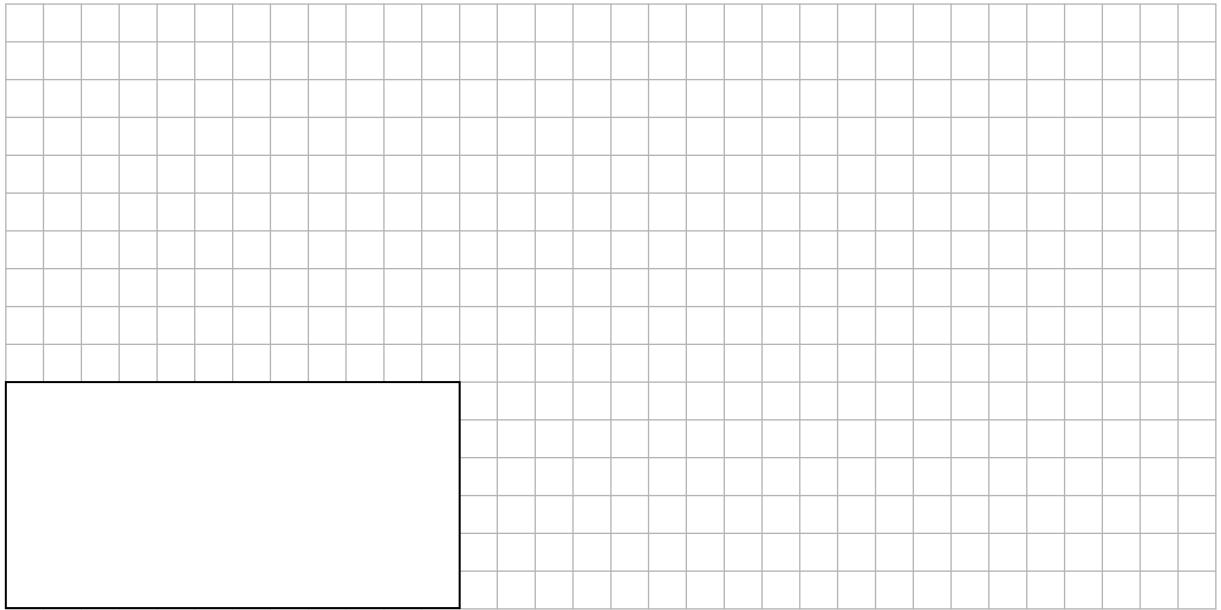
$$-8, \pi, \frac{1}{3}, 6, \sqrt{2}, -4.5 \text{ and } 7^{-1}.$$

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Question 2

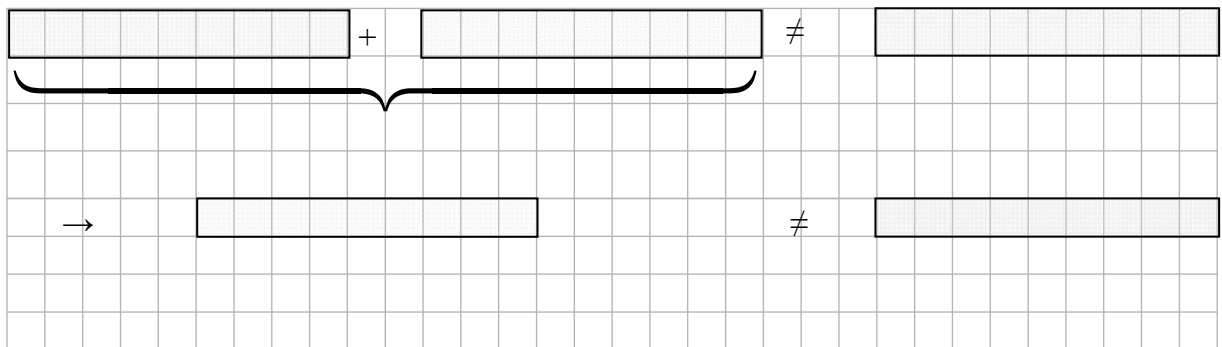
(Suggested maximum time: 5 minutes)

- (a) The diagram below shows three fifths of a rectangle. Complete the rectangle on the grid.



- (b) By shading appropriate sections of the strips below, show that

$$\frac{1}{3} + \frac{2}{6} \neq \frac{3}{9}$$



Question 3 (Suggested maximum time: 10 minutes)

Question 3 (Suggested maximum time: 10 minutes)

The value of one euro against other currencies on a particular day is shown in the table below.

Currency	Rate (€)
US Dollar	1.4045
Pound Sterling	0.87315
Lithuanian Litas	3.4528
Latvian Lats	0.7093
Polish Zloty	4.0440

- (a) Mary was going to America for a few months. She changed €1200 into US Dollars using the exchange rate in the table.

- (i) How many dollars should she receive at this exchange rate?

A blank sheet of graph paper with a grid pattern. The grid consists of small squares formed by thin gray lines. There are 20 columns and 15 rows of squares. The grid is centered on the page, leaving margins at the top, bottom, left, and right.

- (ii) The bank charged 3% commission on the transaction. How many dollars did she receive?

[illegible]

- (b)** On returning to Ireland Mary had \$3060. She changed this amount into euro. The bank again charged her 3% commission on the transaction. She received €2047.

Find the exchange rate on that day, correct to two decimal places.

A full page of blank graph paper with a uniform grid of small squares. The grid consists of 20 columns and 15 rows of squares, totaling 300 squares. The lines are thin and gray, set against a white background. There are no margins or additional markings on the page.

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- [illegible]

£1 = € _____

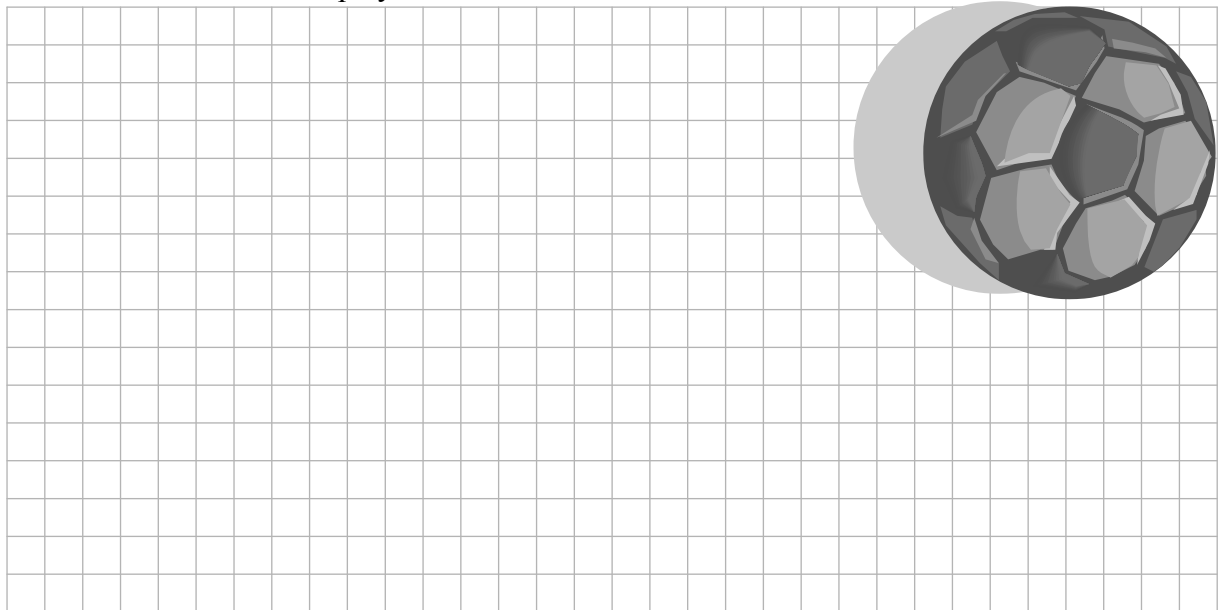
Question 4

(Suggested maximum time: 10 minutes)

A soccer team has three strikers John, Paul and Michael. The number of minutes each had played by the end of a particular season is shown on the table. The team divided a bonus of €150 000 between its strikers in proportion to the time each had played.

Name	Minutes Played
John	2250
Paul	2600
Michael	150

- (a)** Calculate the amount each player received.



- (i)** Calculate the total bonus on offer that season.

[illegible]

Question 5 (Suggested maximum time: 15 minutes)

Question 5 (Suggested maximum time: 15 minutes)

The USC (Universal Social Charge) is calculated on gross income. The rates of the USC are:

- 2% on the first €10 036 of gross annual income
- 4% on the next €5980
- 7% on the balance.

(a) Niamh earned €45 000 in 2011. Find her USC for that year.

A full-page sheet of white graph paper featuring a uniform grid of thin, light gray horizontal and vertical lines. The grid consists of small squares covering the entire area of the page.

The table shows a selection of the tax credits available in Ireland in 2011.

Individual's Tax Credits	Tax Credit 2011
Single Person	€1650
Married or Civil Partner	€3300
Widowed or Surviving Civil Partner	€2190
Home Carer	€810
PAYE	€1650
One Parent Family	€1650

(b) Niamh is a single person who is a PAYE worker. Calculate her total tax credits for 2011.

[illegible]

- (c) The standard rate of tax is 20% and the higher rate is 41%. The Standard Rate Cut-off Point for a single person is €32 800. Calculate Niamh's tax bill for 2011.

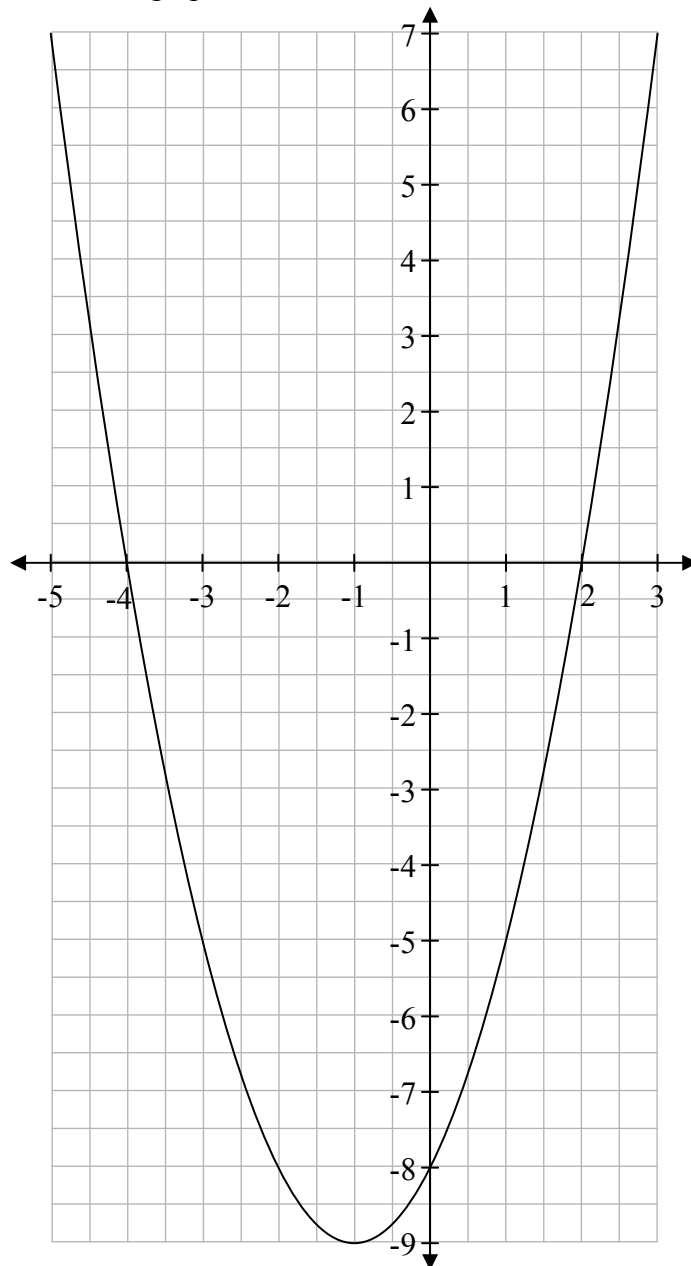
[illegible]

- (d)** Calculate Niamh's net pay for the year, after tax and USC are paid.

Question 6

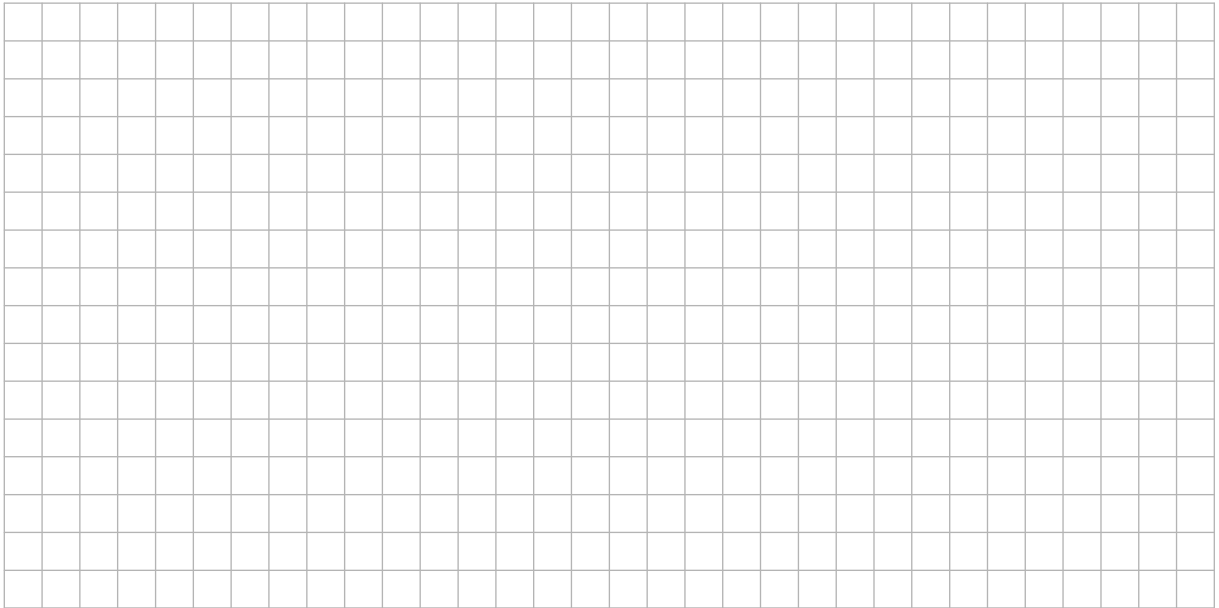
(Suggested maximum time: 15 minutes)

A group of four students is studying graphs of functions of the form $f : x \mapsto x^2 + 2x + k$, $x \in \mathbb{R}$. Each takes an integer value of k and draws the graph of their function in a suitable domain. Maria took $k = -8$ and drew the graph below.

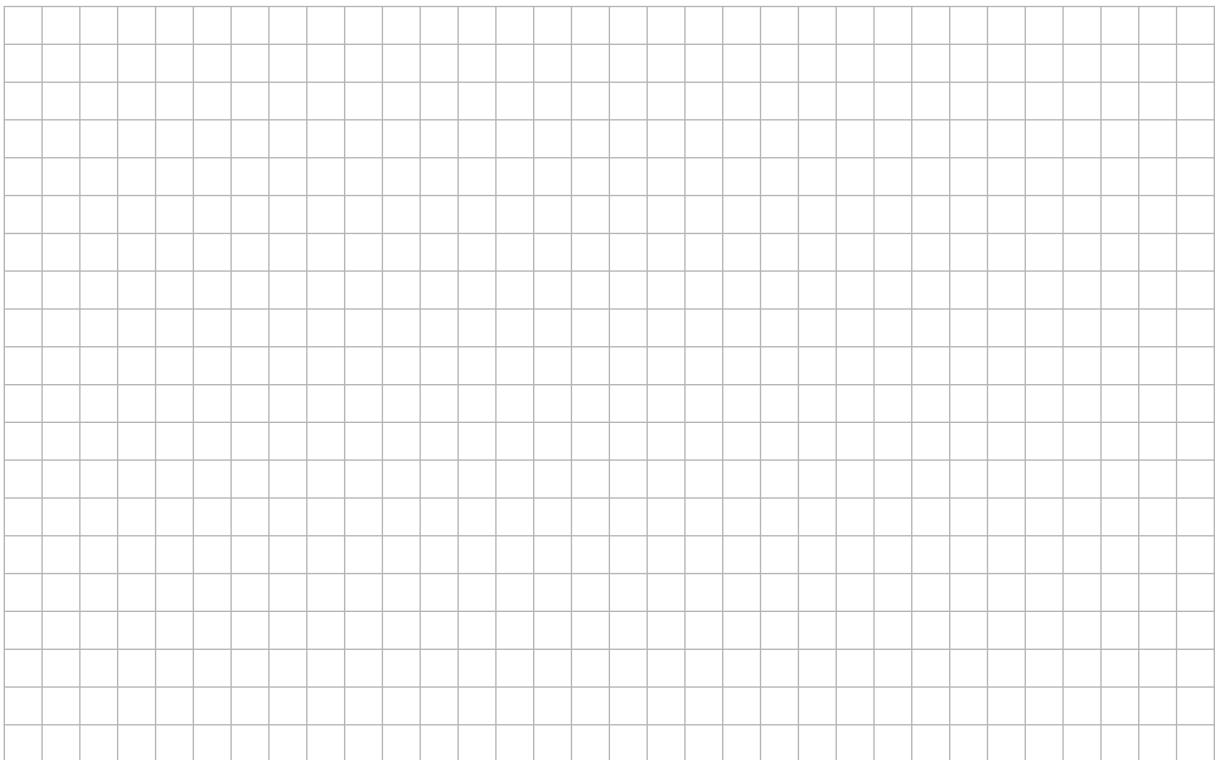


- (a)** Use the graph to write down the roots of the equation $x^2 + 2x - 8 = 0$.

- (b)** Keith's graph passes through the point $(3, 2)$. Find the value of k that Keith used.



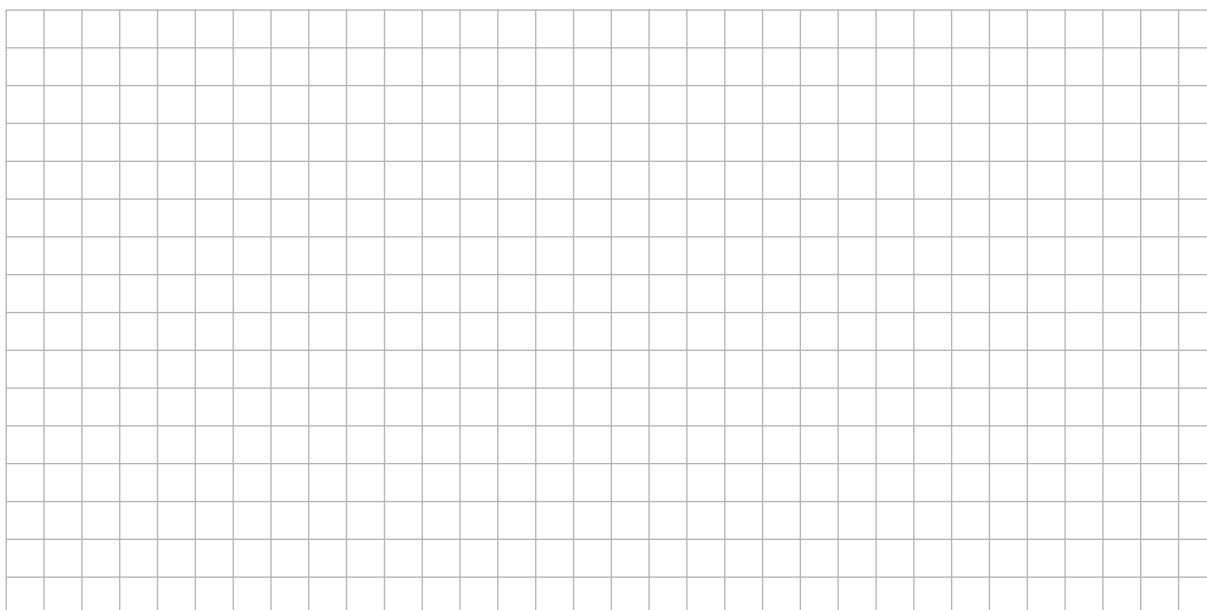
- (c)** On Alice's graph, the two roots of the function are the same. Find the value of k that Alice used.



- (d)** Draw a sketch of Alice's function on the diagram shown in part **(a)**.

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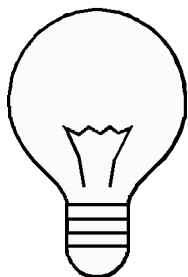
- (e) Emma's graph shows that the roots of her function are -5 and 3 . Find the value of k that she used.



Question 7

(Suggested maximum time: 20 minutes)

Lisa is on a particular payment plan called “Plan A” for her electricity. She pays a standing charge each month even if no electricity is used. She also pays a rate per unit used. The table shows the cost, including the standing charge, of using different amounts of units, in a month.



Units Used	Plan A Cost in euro
100	38
200	56
300	74
400	92
500	110
600	128
700	146
800	164

- (a) Use the data in the table to show that the relationship between the number of units used and the cost is linear.



-
- The graph is a blank coordinate system with a grid. The horizontal axis (x-axis) is labeled "Units Used" and has major tick marks at 100, 200, 300, 400, 500, 600, 700, and 800. The vertical axis (y-axis) is labeled "Cost in euro" and has major tick marks at 10, 20, 30, 40, 50, 60, 70, 80, 90, 100, 110, 120, 130, 140, and 150. The grid consists of 8 vertical lines and 16 horizontal lines.

- (d)** Write down a different method of finding the standing charge. Find the standing charge using your method.

Method: _____

Standing charge: _____

Project Maths, Phase 2
Paper 1 – Higher Level

- [illegible]

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- A full-page sheet of graph paper featuring a uniform grid of small squares. The grid consists of 20 columns and 20 rows, creating a total of 400 square units. The lines are thin and light gray, set against a white background. There are no margins, text, or other markings on the page.

Question 8 (Suggested maximum time: 5 minutes)

Question 8 (Suggested maximum time: 5 minutes)

A capacitor is a device which stores electricity. The formula $W = \frac{1}{2}CV^2$ gives the energy stored in the capacitor, where W is the energy, C is the capacitance and V is the voltage, and standard units are used throughout.

- (a)** Find the amount of energy stored in a capacitor when $C = 2500$ and $V = 32$.

[illegible]

- (b)** Write V in terms of W and C .

[illegible]

Question 9 (Suggested maximum time: 10 minutes)

Question 9 (Suggested maximum time: 10 minutes)

Consideration is being given to changing the number of points a team gets for a win and also the number of points a team gets for a draw in a soccer league. No points will be awarded for a loss. The table below shows the standing of two teams after six games under the proposed new system.

Team	Played	Won	Drawn	Lost	Points (new system)
Team A	6	2	2	2	12
Team B	6	1	5	0	10

- (a)** Find the number of points which would be awarded for **(i)** a win and **(ii)** a draw under this proposed system.

This image shows a full page of blank graph paper. The background is a very light gray, and it is covered by a grid of thin, darker gray lines. The grid consists of small, equal-sized squares that extend across the entire width and height of the page, leaving a small margin at the top and bottom. There are no markings, text, or drawings on the grid.

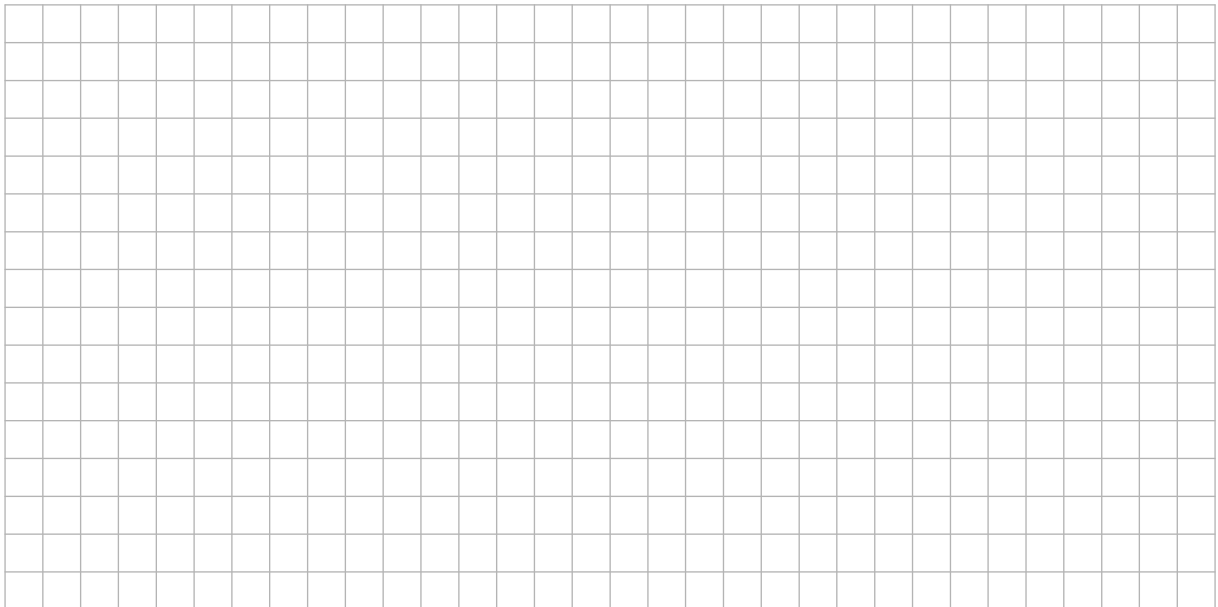
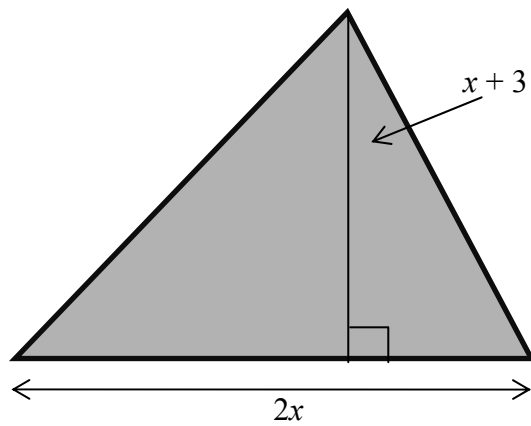
- (b)** The current system awards 3 points for a win and 1 point for a draw. Suggest one reason why it might be preferable to change to the system proposed in part **(a)**.

A full-page sheet of white graph paper featuring a uniform grid of thin, light gray horizontal and vertical lines. The grid consists of small squares covering the entire area of the page.

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Question 10**(Suggested maximum time: 5 minutes)**

A triangle has a base length of $2x$ cm and a perpendicular height of $(x + 3)$ cm.
The area of the triangle is 10 cm^2 . Find the distance x .



Question 11

(Suggested maximum time: 5 minutes)

Factorise fully each of the following expressions:

(i) $5x^3 - 10x^2$

(ii) $4x^2 - 81y^2$

[illegible]

(iii) $a^2 - ab + 3a - 3b$

Question 12

(Suggested maximum time: 10 minutes)

(a) Solve each of the following equations:

(i) $x^2 - 5x - 6 = 0$

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Question 13

(Suggested maximum time: 5 minutes)

For real numbers a , b and c , complete the table below. Indicate whether each statement is always true, never true or sometimes true.

Statement	Always true	Never true	Sometimes true
If $a > b$ and $b > c$, then $a > c$			
If $-a < 4$ and $b < -4$, then $a < b$			
If $a > b$, then $-a > -b$			
If $a > b$ and $b < c$, then $a < c$			
If $3a + 1 > 2$, then $a > 0$			
If $2b - 4 < 3b - 8$, then $b > 4$			
If a and b are both positive and $a < b$, then $\frac{1}{a} < \frac{1}{b}$			

Question 14

(Suggested maximum time: 20 minutes)

Let g be the function $g : x \mapsto 2^{x-3}$.

- (a) Find the value of $g(3)$.

- (b)** Let h be the function $h : x \mapsto x^2 - 3x$.

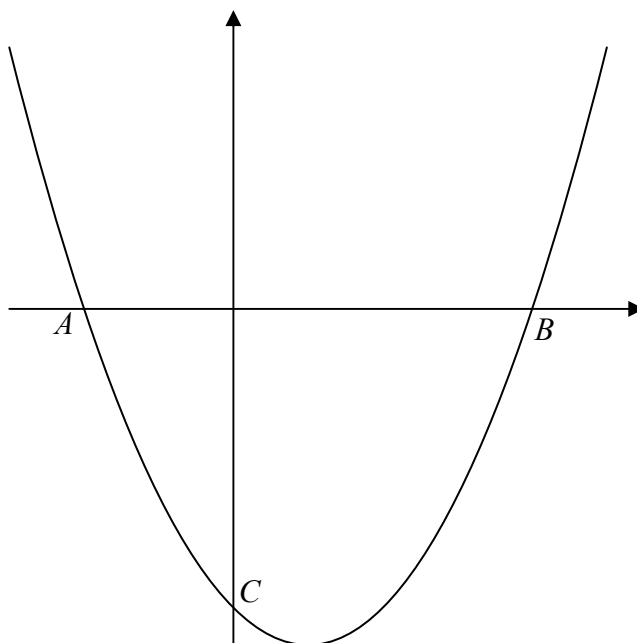
- (i) Express $h(t)$ and $h(2t + 1)$ in terms of t .

- (ii)** Hence, find the values of t for which $h(t) = h(2t + 1)$.

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- (c) The diagram shows part of the graph of the function $f : x \mapsto x^2 - 2x - 8$, $x \in \mathbb{R}$.



The graph intersects the x -axis at A and B , and the y -axis at C .

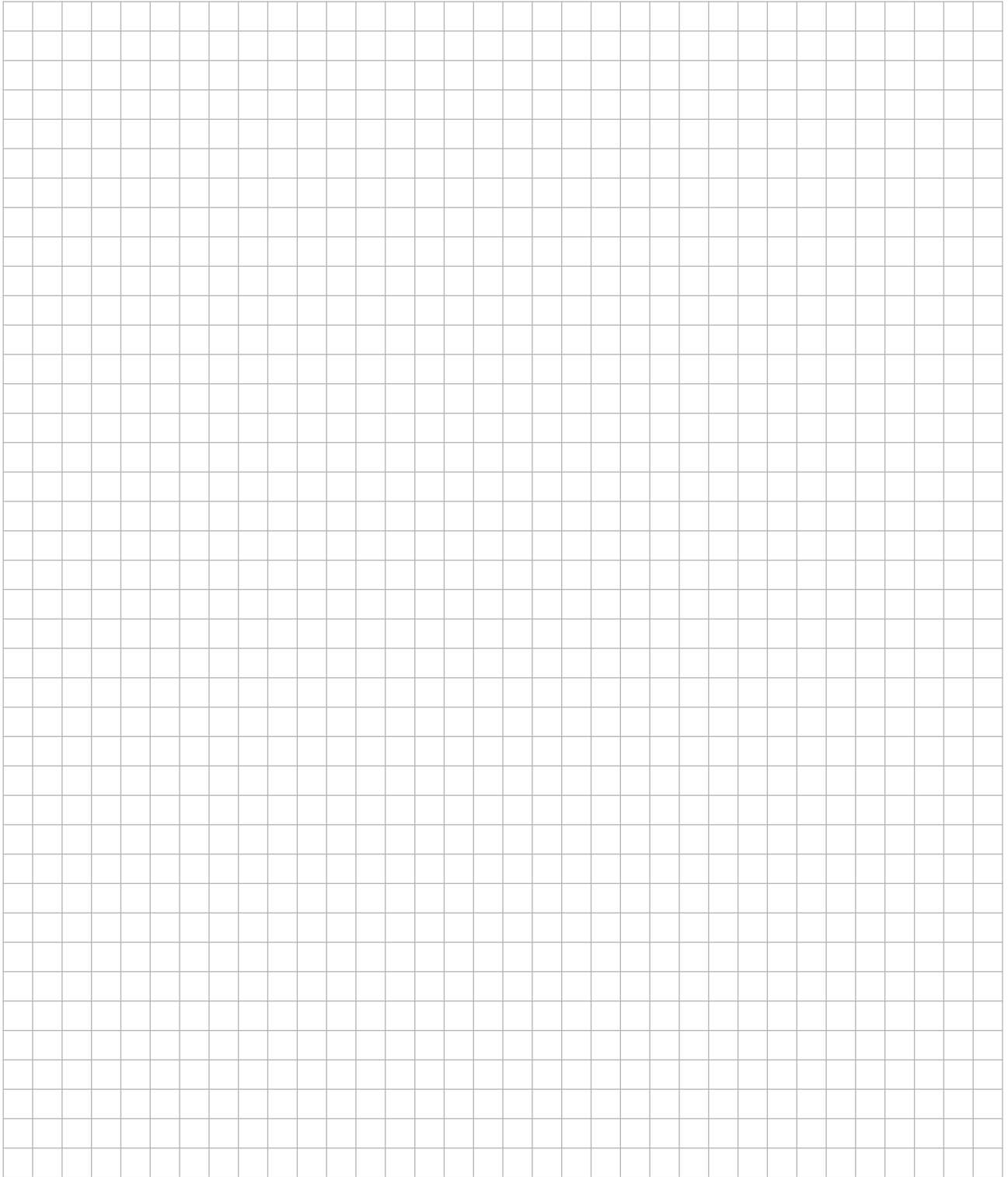
- (i) Find the co-ordinates of A , B and C .



- (ii) Hence, write down the range of values of x for which $x^2 - 2x - 8 \leq 0$.



Project Maths, Phase 2
Paper 1 – Higher Level



Junior Certificate 2012 – Higher Level

Mathematics (Project Maths – Phase 2) – Paper 1

Friday 8 June

Afternoon 2:00 to 4:30