

2019.M27



2019L003G1EL



Coimisiún na Scrúduithe Stáit
State Examinations Commission

Leaving Certificate Examination 2019

Mathematics

Paper 1

Ordinary Level

Friday 7 June – Afternoon 2:00 to 4:30

300 marks

Examination Number

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Centre Stamp

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2019L003G1EL0128

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Instructions

There are **two** sections in this examination paper.

Section A	Concepts and Skills	150 marks	6 questions
Section B	Contexts and Applications	150 marks	3 questions

Answer all nine questions.

Write your Examination Number in the box on the front cover.

Write your answers in blue or black pen. You may use pencil in graphs and diagrams only.

This examination booklet will be scanned and your work will be presented to an examiner on screen. Anything that you write outside of the answer areas may not be seen by the examiner.

Write all answers into this booklet. There is space for extra work at the back of the booklet. If you need to use it, label any extra work clearly with the question number and part.

The superintendent will give you a copy of the *Formulae and Tables* booklet. You must return it at the end of the examination. You are not allowed to bring your own copy into the examination.

You will lose marks if your solutions do not include relevant supporting work.

You may lose marks if you do not include appropriate units of measurement, where relevant.

You may lose marks if you do not give your answers in simplest form, where relevant.

Write the make and model of your calculator(s) here:



Answer **all six** questions from this section.

Question 1**(25 marks)**

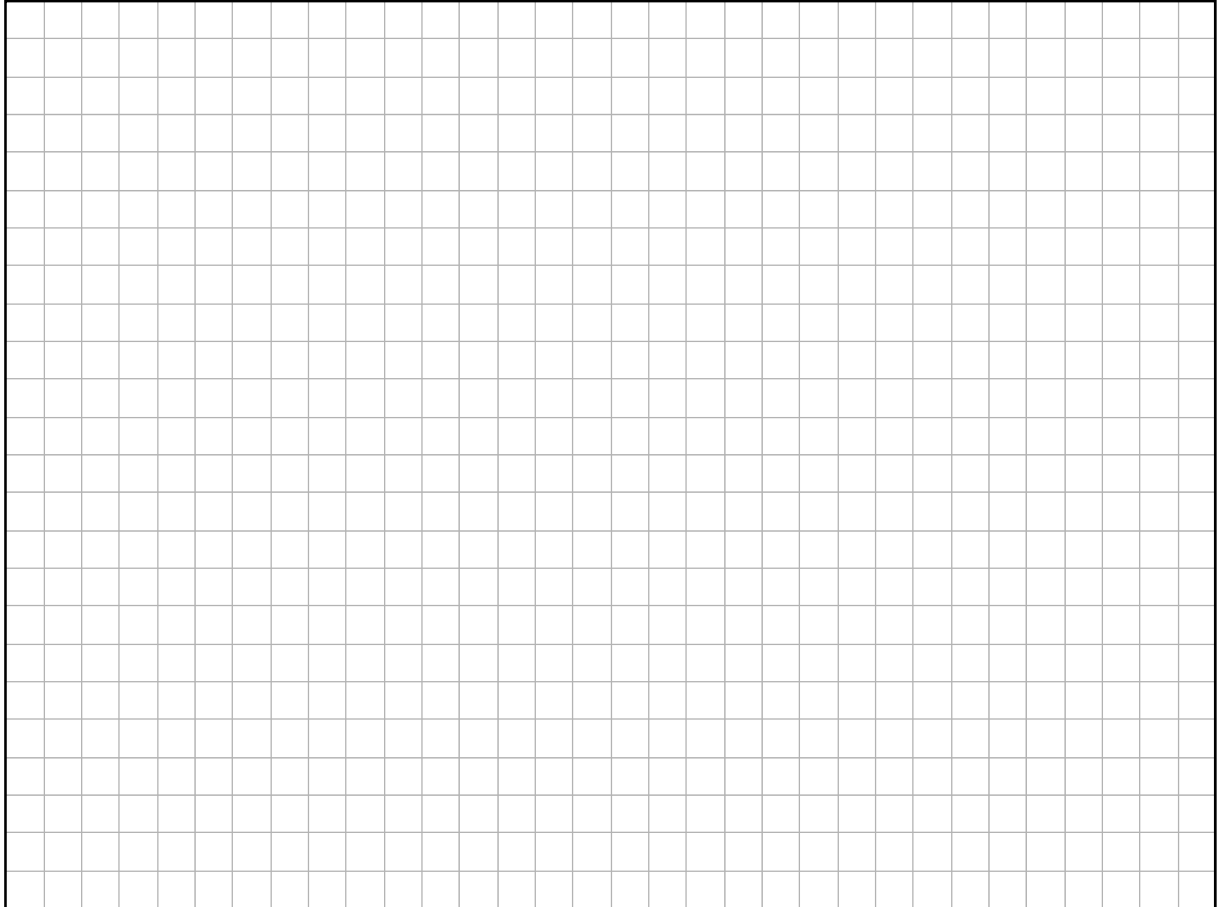
Eimear earns a gross wage of €40 000 per annum with Company A.

- (a) Eimear pays income tax at a rate of 20% on income up to the standard rate cut-off point of €35 300. She pays tax at a rate of 40% on the remainder. She has annual tax credits of €1650. Find how much income tax she pays per annum.

- (b) Eimear pays her health insurance which costs her €1500 net. Find her annual income after paying income tax and health insurance (i.e. her net annual income).



- (c) Eimear is planning to change jobs. She is offered a job by Company B with a gross wage of €38 000 and a bonus of €1500 (tax free to Eimear) to be paid by the company, which she would use to pay her health insurance. Her tax rates and credits would remain the same. Find by how much Eimear's net annual income (after paying income tax and health insurance) will increase if she accepts the job with Company B.



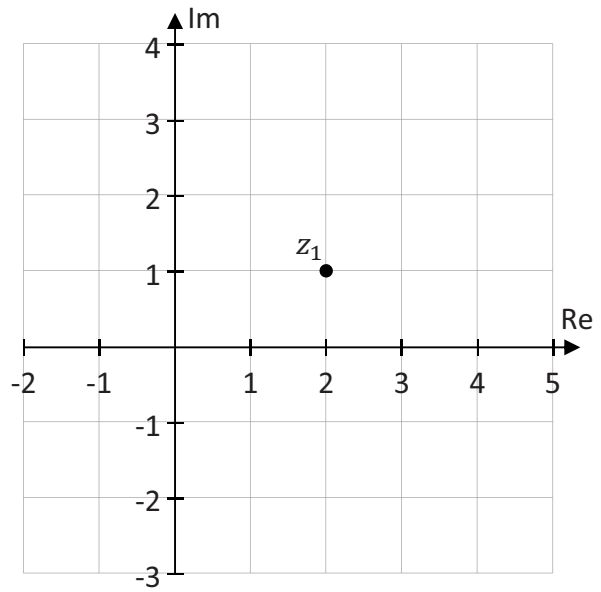
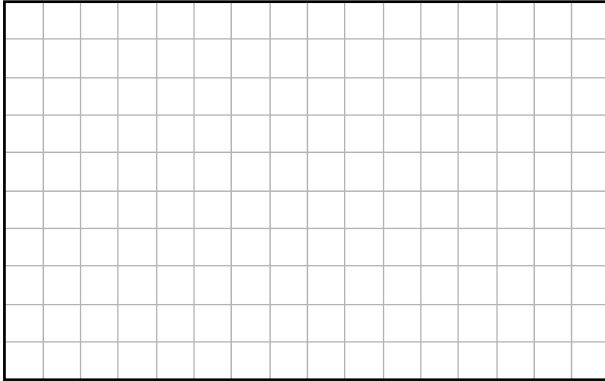
Question 2

(25 marks)

The complex number $z_1 = 2 + i$, where $i^2 = -1$, is shown on the Argand Diagram below.

(a) (i) $z_2 = 2z_1$.

Find the value of z_2 , and **plot and label** it on the Argand Diagram.

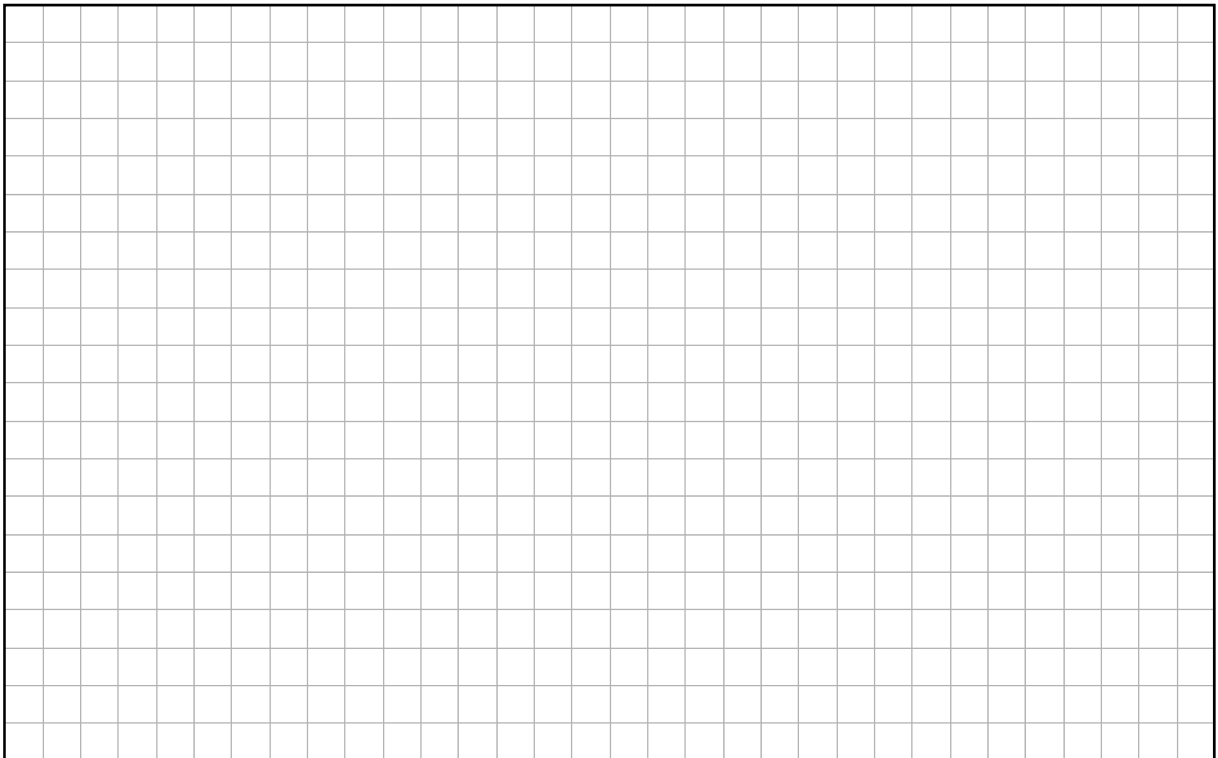


(ii) \bar{z}_1 is the complex conjugate of z_1 .

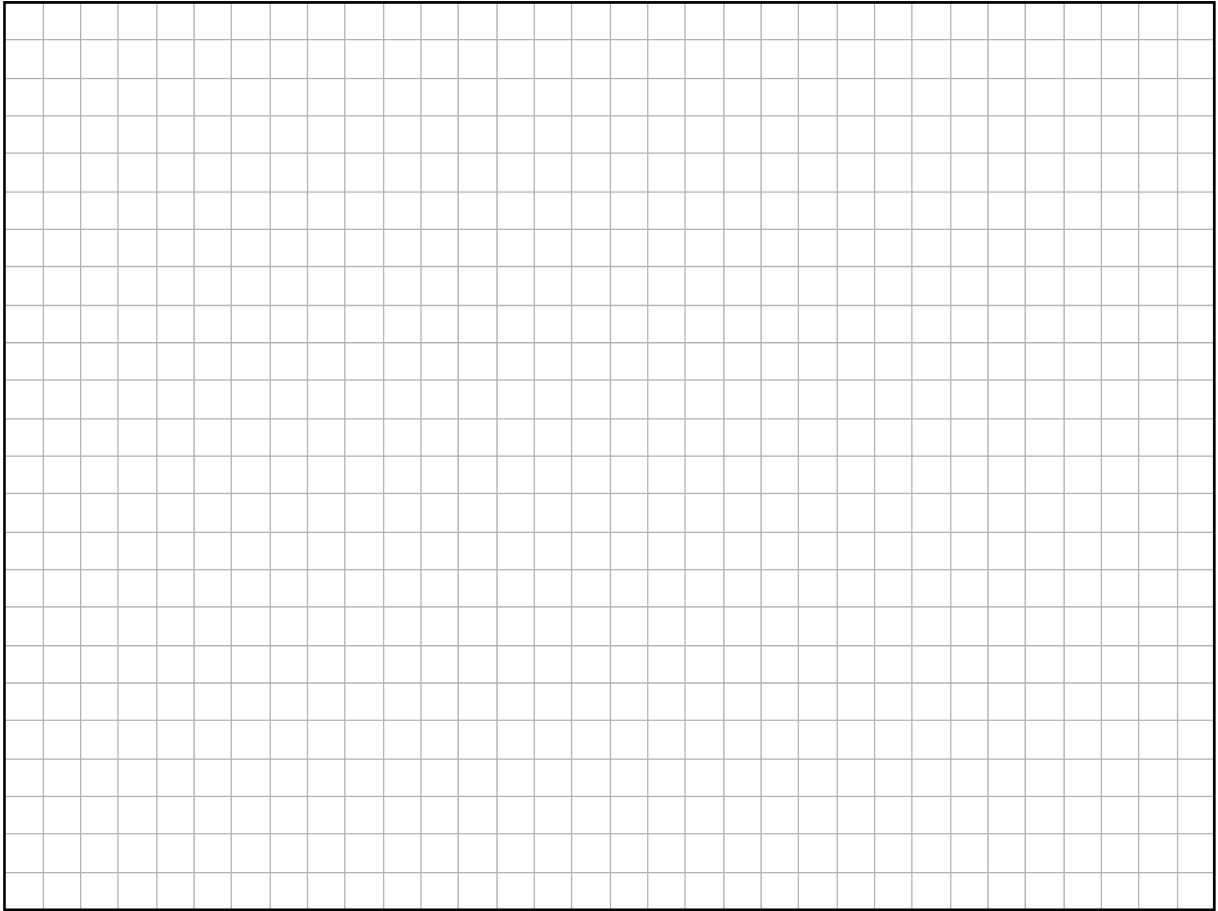
Write down the value of \bar{z}_1 , and **plot and label** it on the Argand Diagram.

$\bar{z}_1 =$

(iii) Investigate if $|z_2| = |z_1 + \bar{z}_1|$.



(b) Show that $z_1 = 2 + i$ is a solution of the equation $z^2 - 4z + 5 = 0$.



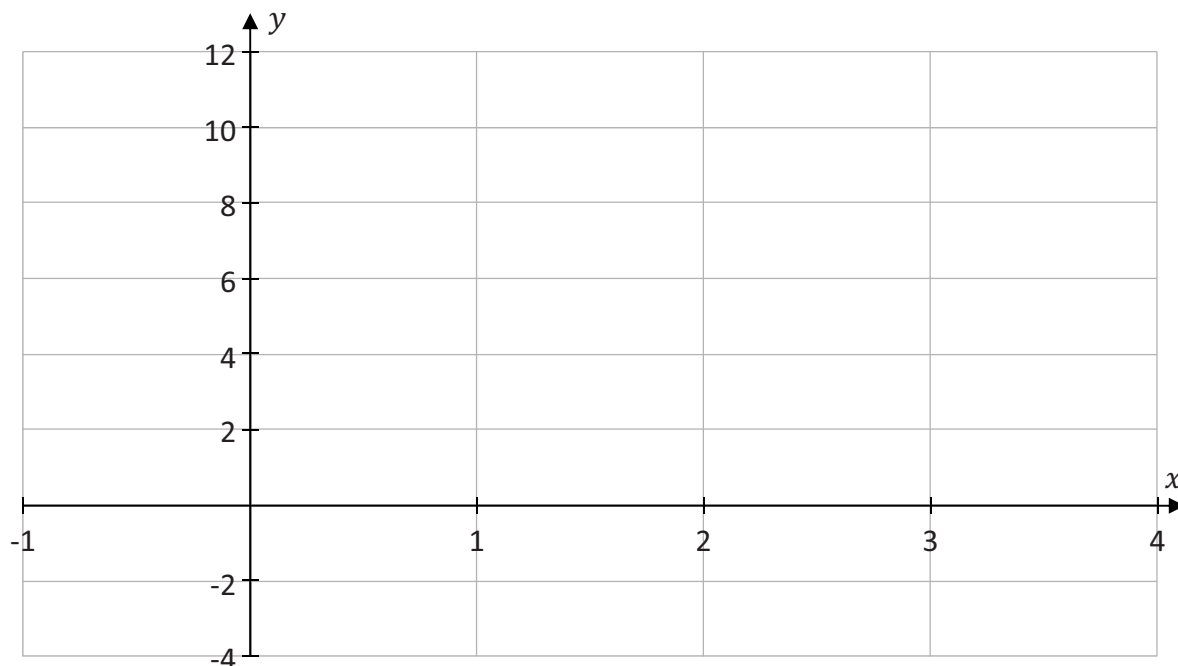
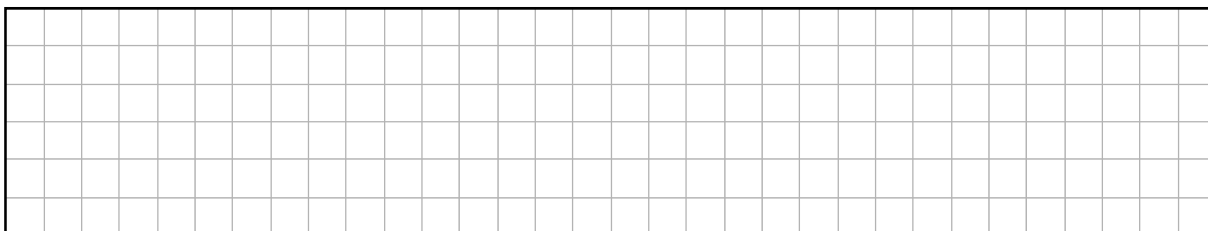
Question 3

(25 marks)

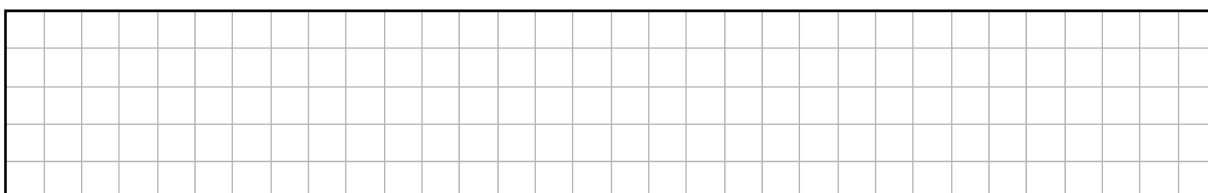
The function f is defined as $f(x) = -x^3 + 4x^2 + x - 2$, where $x \in \mathbb{R}$.

- (a) (i) Complete the table below for the values of f in the domain $-1 \leq x \leq 4$ and hence draw the graph of the function $f(x)$ in the domain $-1 \leq x \leq 4, x \in \mathbb{R}$.

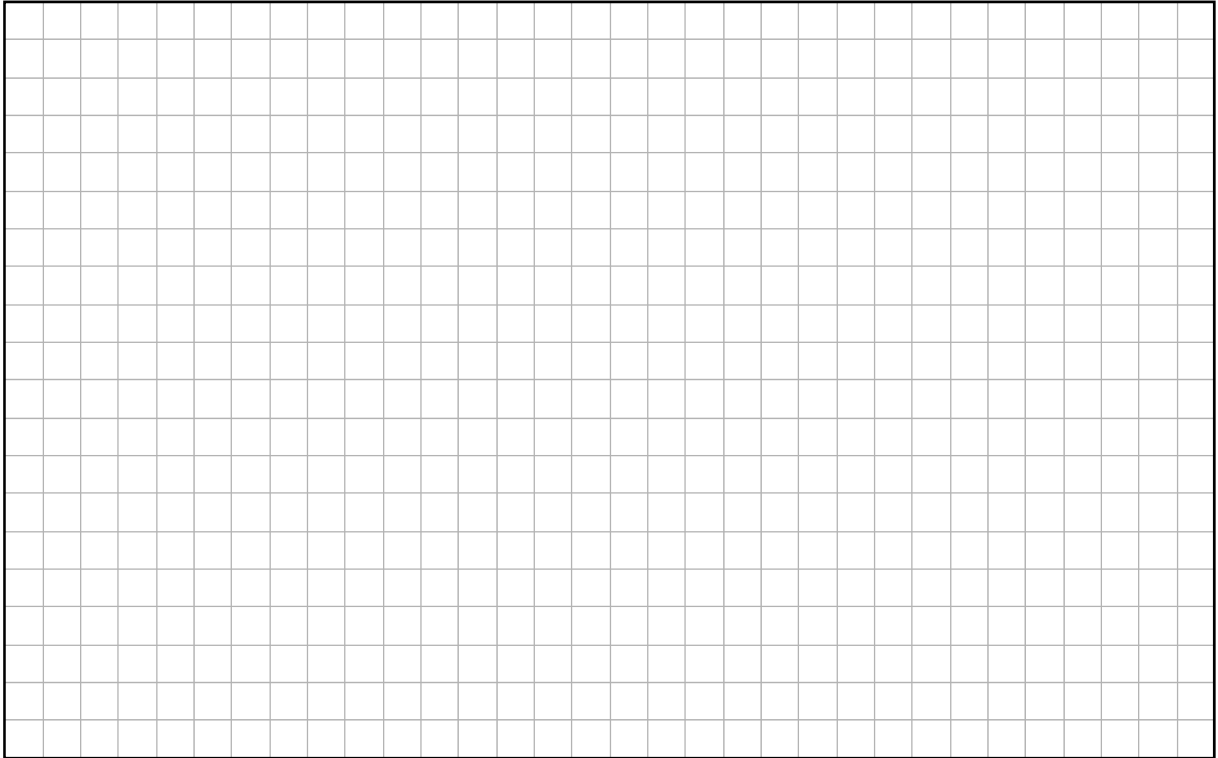
x	-1	0	1	2	3	4
$f(x)$					10	



- (ii) Use your graph to estimate the two roots of $f(x)$ which are in the domain $-1 \leq x \leq 4$.



(b) Find the value of x for which $f''(x) = 0$, where $f''(x)$ is the second derivative of $f(x)$.

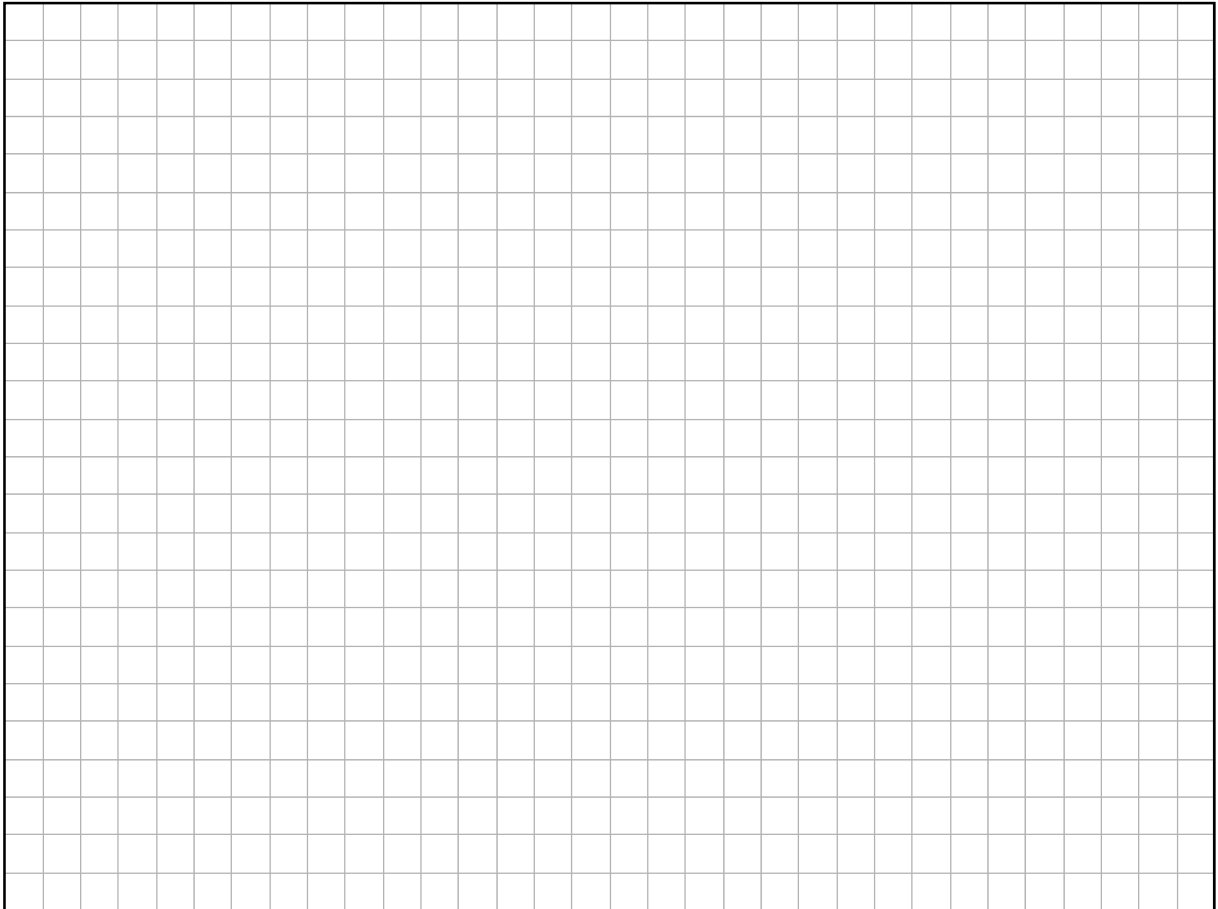


Question 4

(25 marks)

(a) Solve for x :

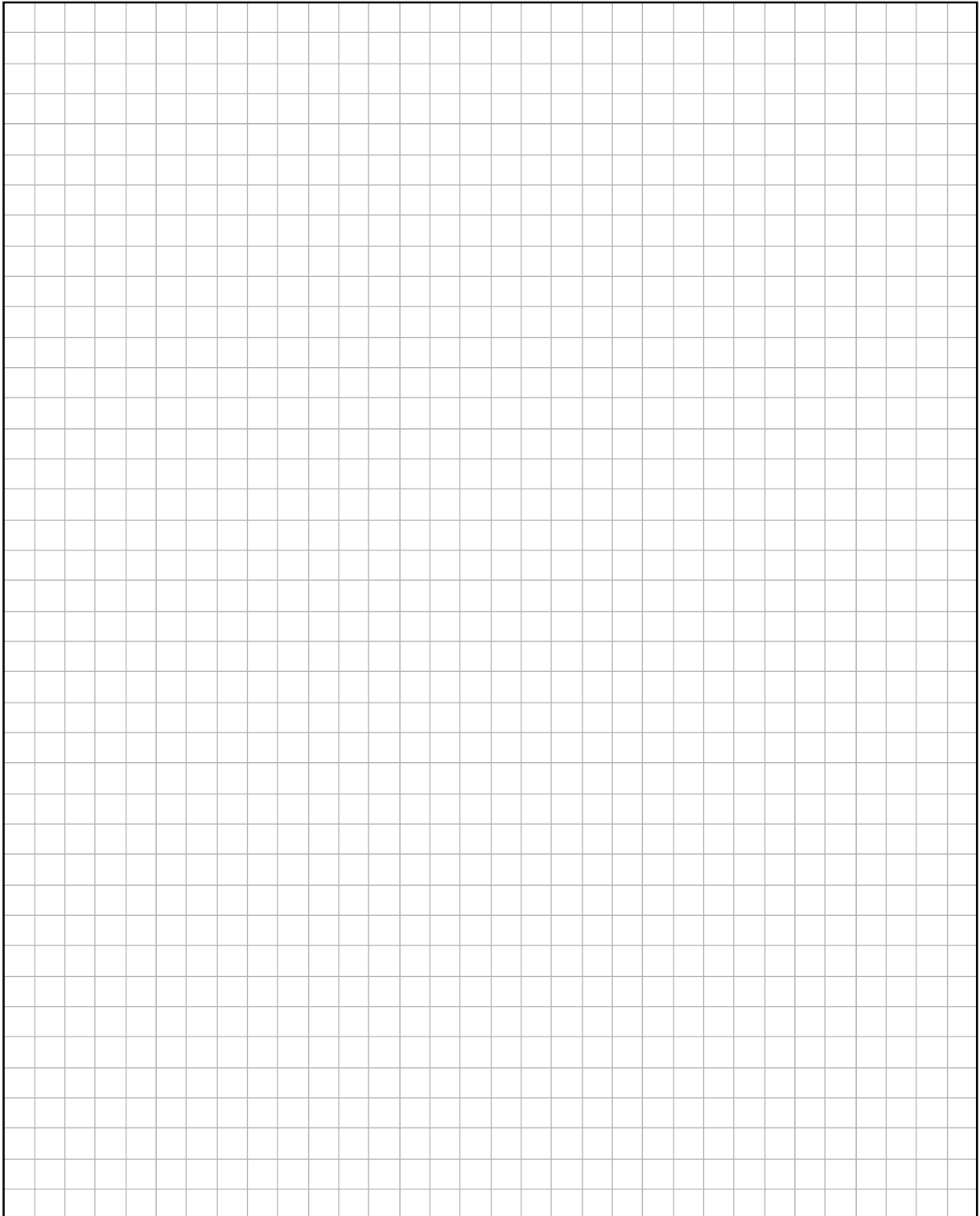
$$\frac{3x + 1}{5} + \frac{x - 2}{2} = \frac{47}{10}$$



(b) Solve the simultaneous equations:

$$x - 5y = -13$$

$$x^2 + y^2 = 13.$$



Question 5

(25 marks)

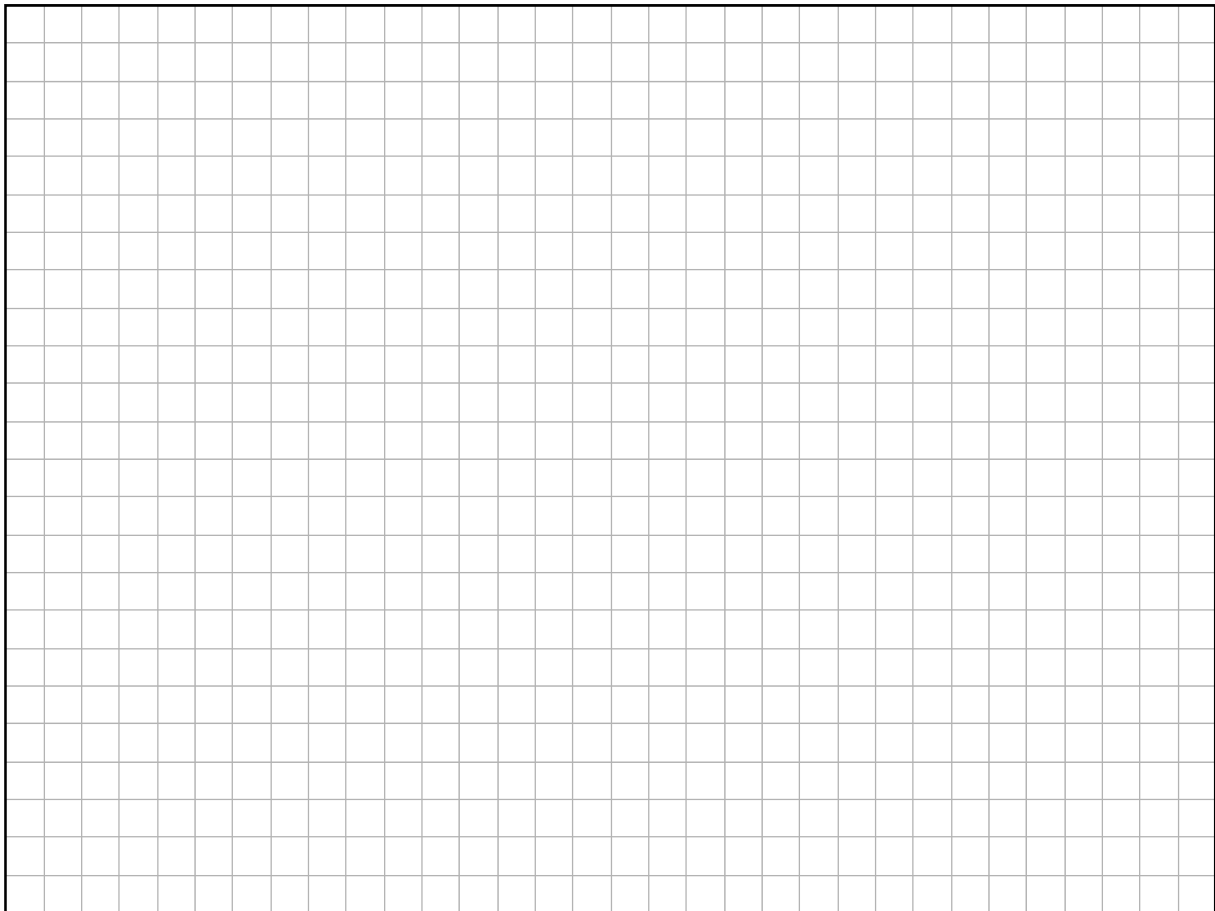
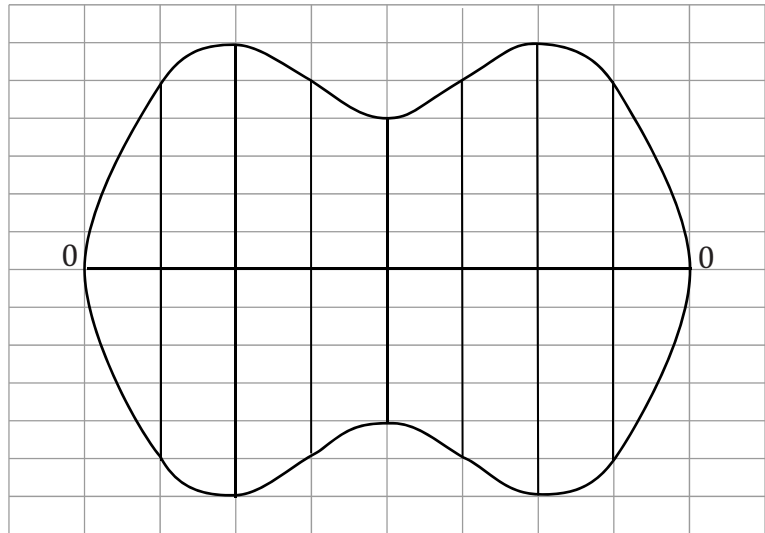
Harry draws a scale diagram of the portion of his garden that is covered in lawn.
His diagram is shown below.

Each box on the grid is $1\text{ cm} \times 0.5\text{ cm}$.

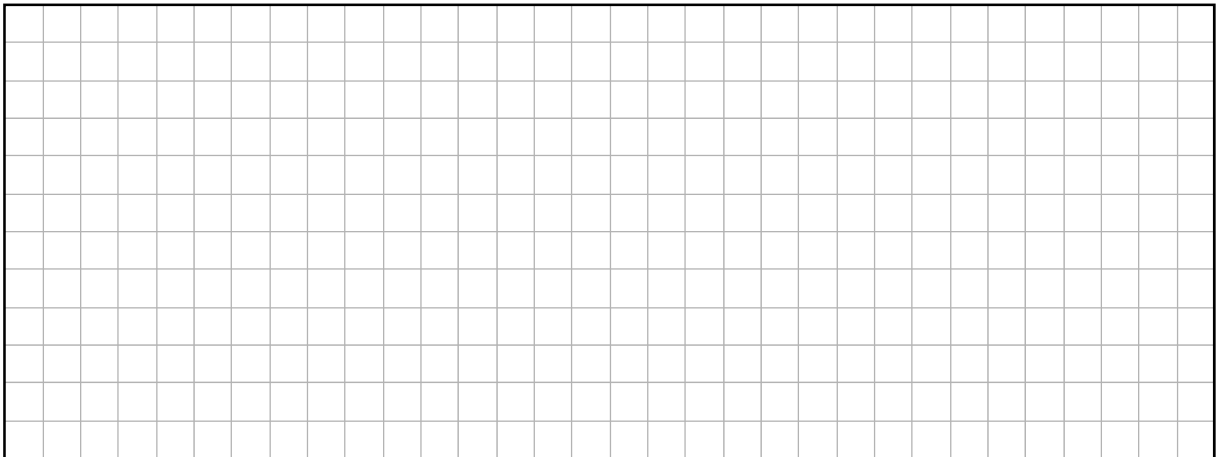
Each cm on Harry's diagram represents 3 m.

In order to estimate the area of the lawn Harry divides the diagram into eight sections.

- (a)** Use the trapezoidal rule to estimate the area of the lawn using the scale: $1\text{ cm} = 3\text{ m}$.



- (b) Nuala can walk at a speed of 1.6 metres per second.
Write this speed in kilometres per hour.

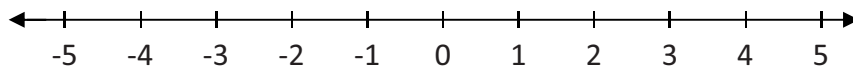
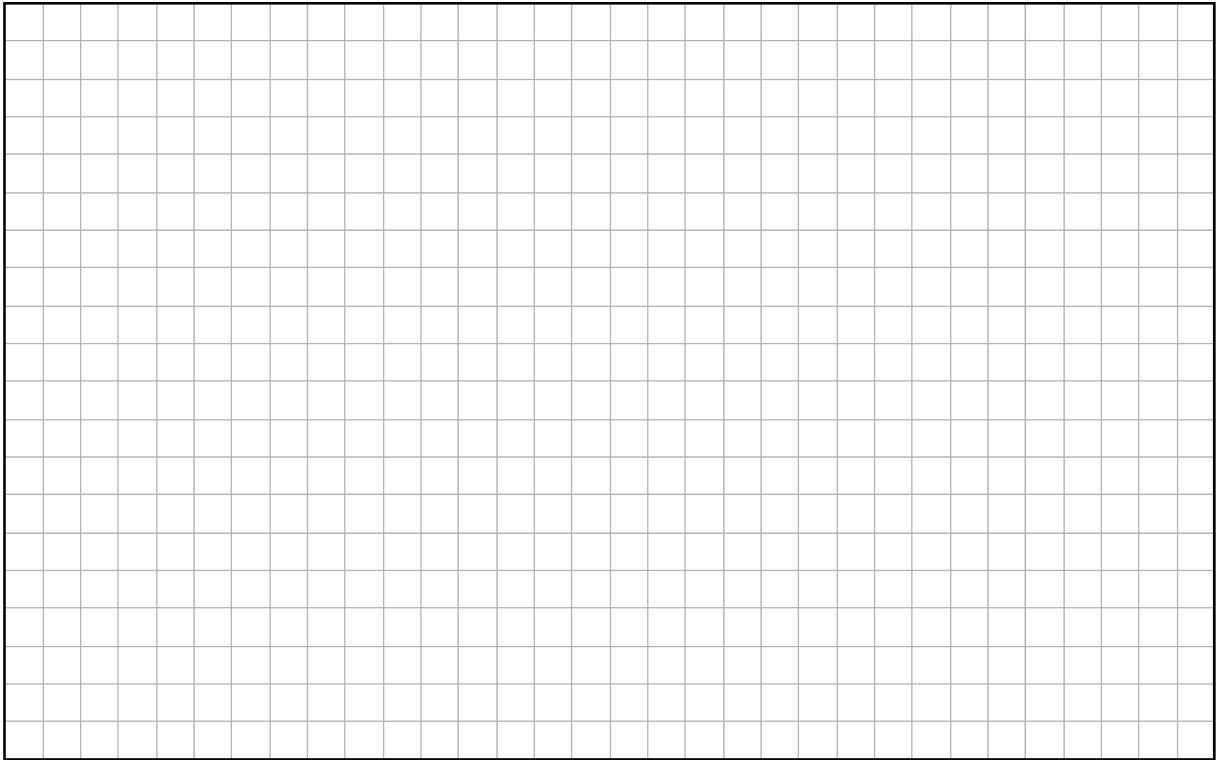
A large rectangular grid consisting of 20 columns and 15 rows of small squares, intended for the student to write their answer to the problem.

Question 6

(25 marks)

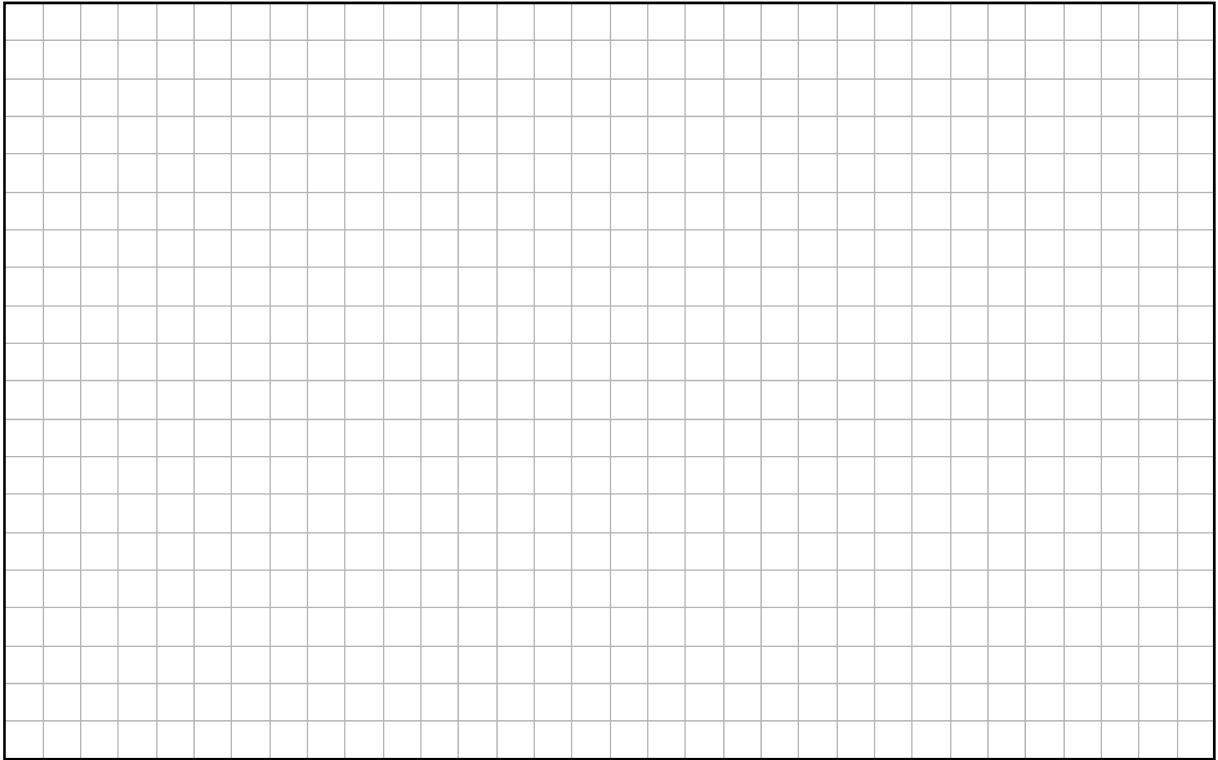
(a) Solve the following inequality for $x \in \mathbb{R}$ and show your solution on the numberline below:

$$2(3 - x) < 8.$$

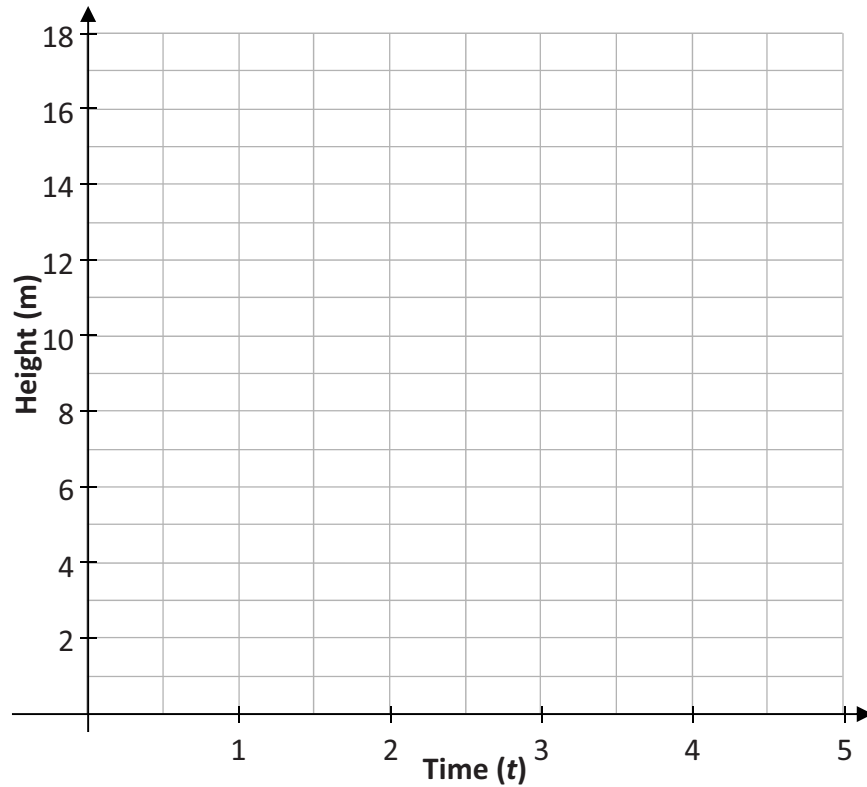


(b) Solve for x :

$$2^{2x-1} = 64.$$

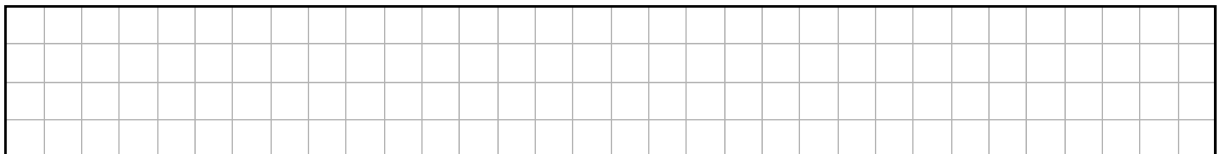


(ii) On the grid below draw a graph to show the height of the ball while it was in the air.

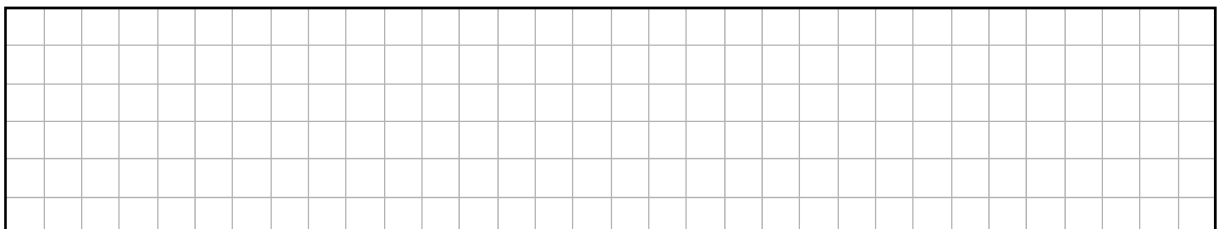


(c) Use your graph to estimate:
(Show your work on the graph above)

(i) the length of time the ball was in the air from the time it was hit until it landed on the ground



(ii) the length of time the ball was 10 m, or more, above the ground.



This question continues on the next page.

- (d) (i) Find $f'(t)$, the derivative of $f(t) = -4t^2 + 16t + 1$.

- (ii) Use your answer from **part (d)(i)** to find the speed of the ball when it had been in the air for 4 seconds. Give your answer in metres per second.

- (iii) Use your answer from **part (d)(i)** to find the value of t for which the ball was descending and travelling at a speed of 8 metres per second.



Question 8**(55 marks)**

(a) The power (P) of an engine is measured in horsepower using the formula:

$$P = \frac{R \times T}{5252}$$

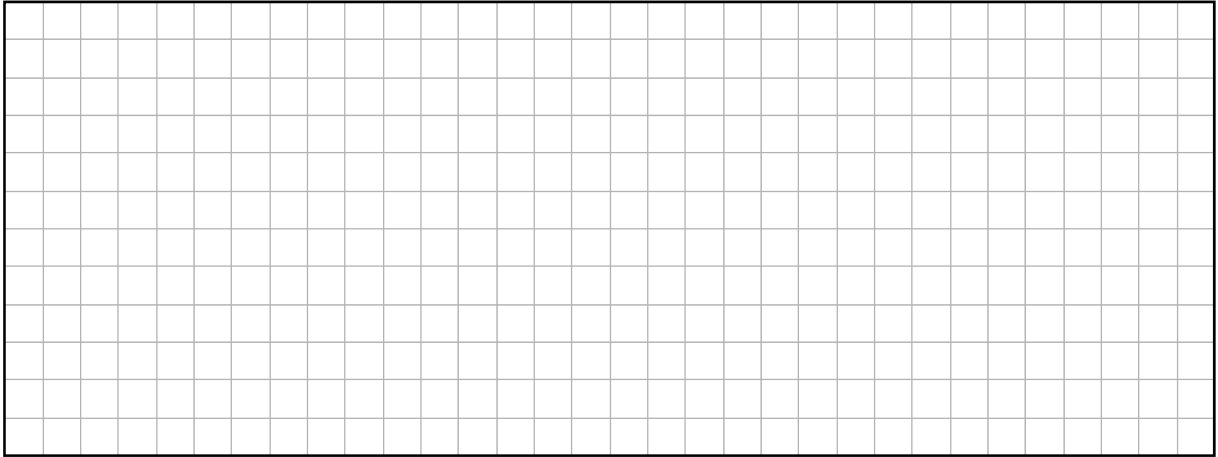
where R is the engine speed measured in revolutions per minute (RPM) and T is the torque measured in appropriate units.

- (i) Find the power of an engine that generates 480 units of torque at 2500 RPM. Give your answer correct to the nearest whole number.

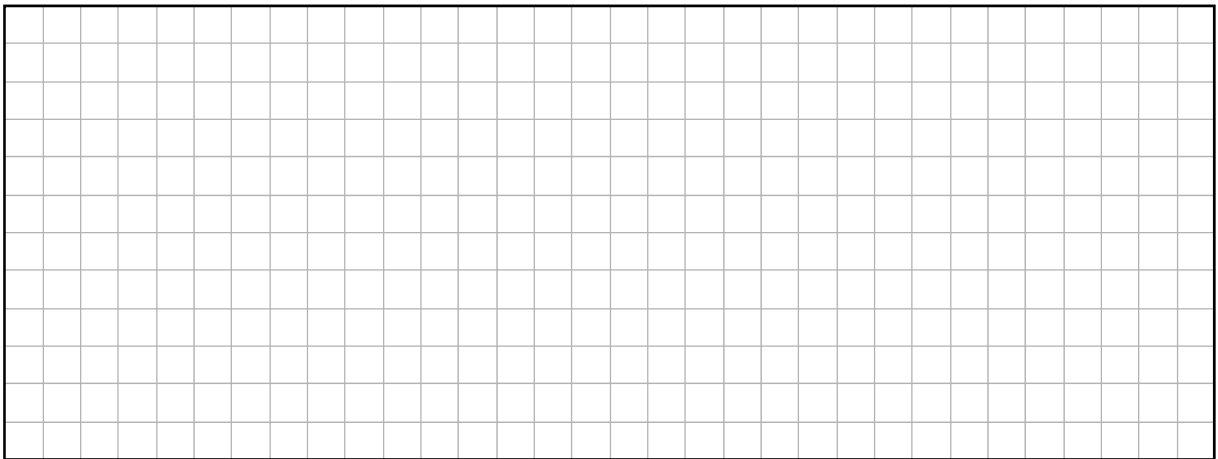
- (ii) Rearrange the formula to write R in terms of P and T .

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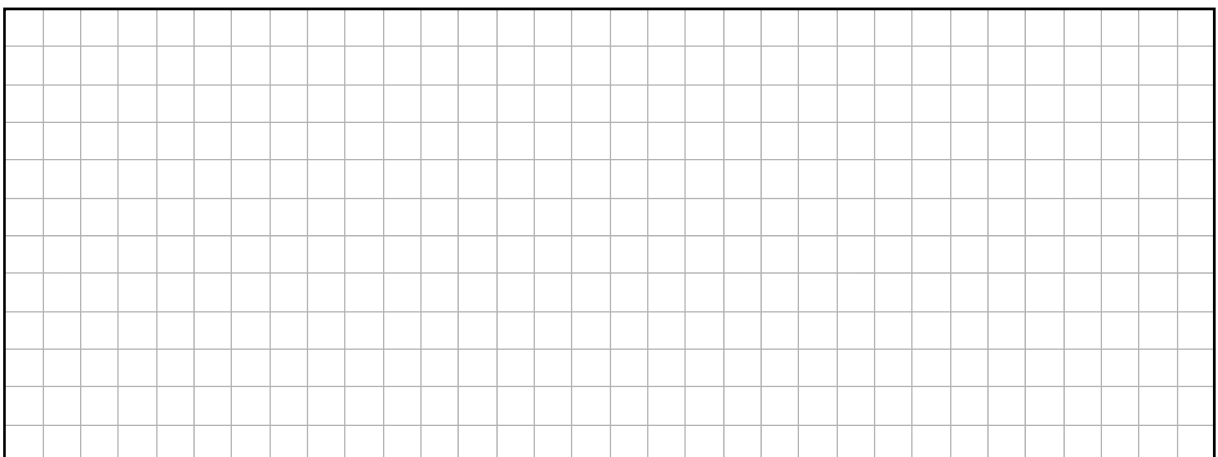
(iv) Find the month in which the company breaks even (i.e. €0 profit).



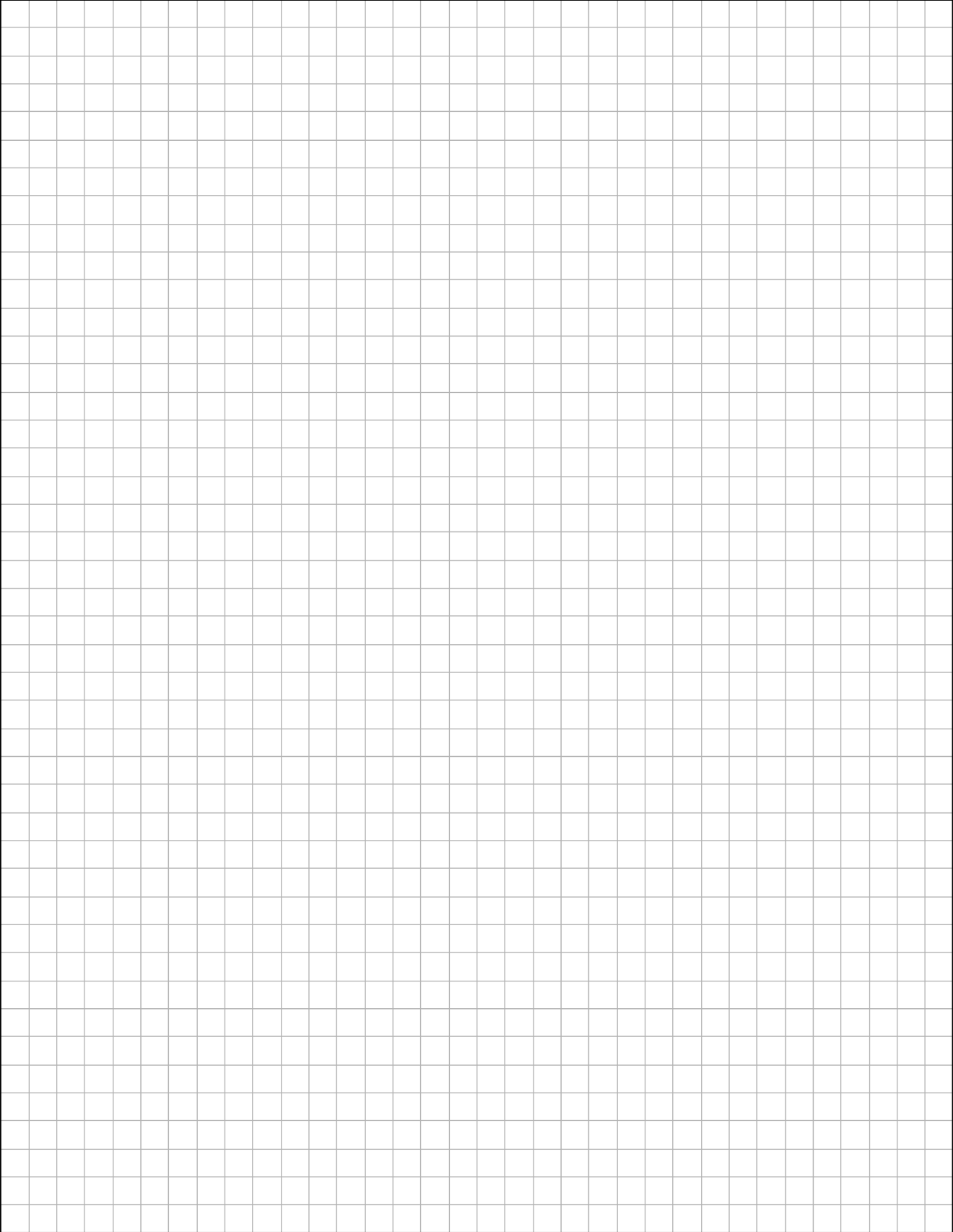
(v) Find S_n , the general term for the **total** profit of the company after n months.



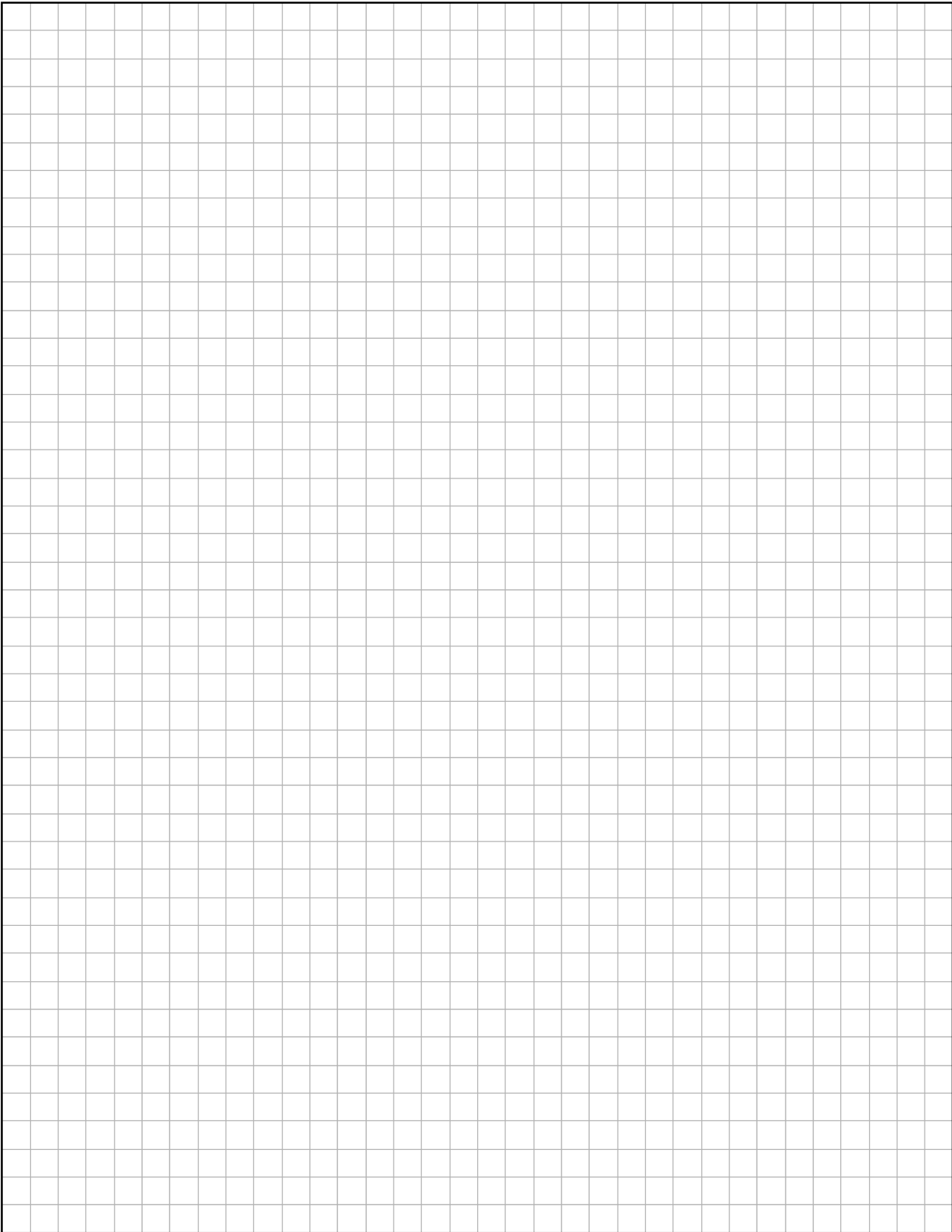
(vi) Hence, or otherwise, find the total profit of the company at the end of January 2019 (i.e. month 37).



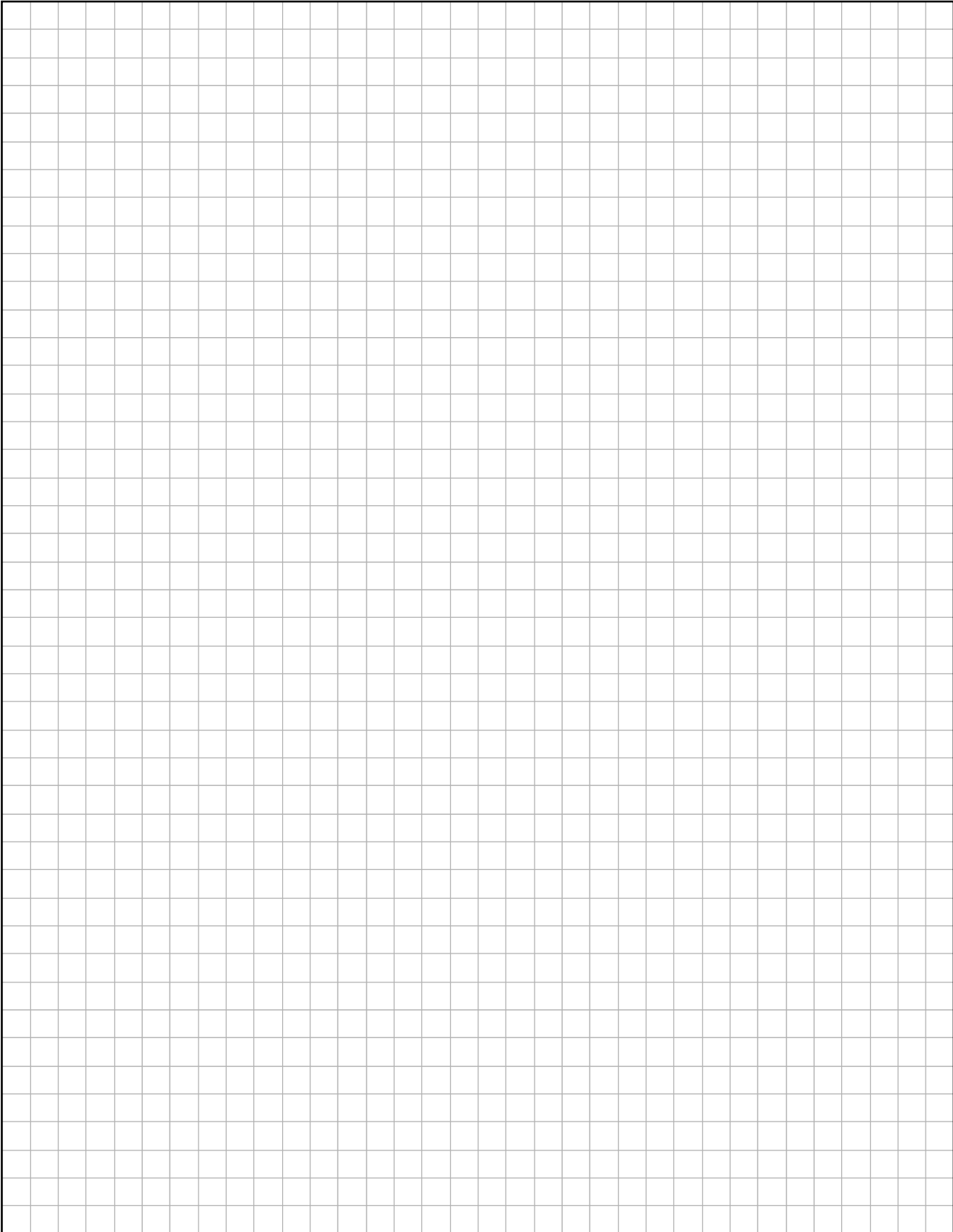
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Label any extra work clearly with the question number and part.



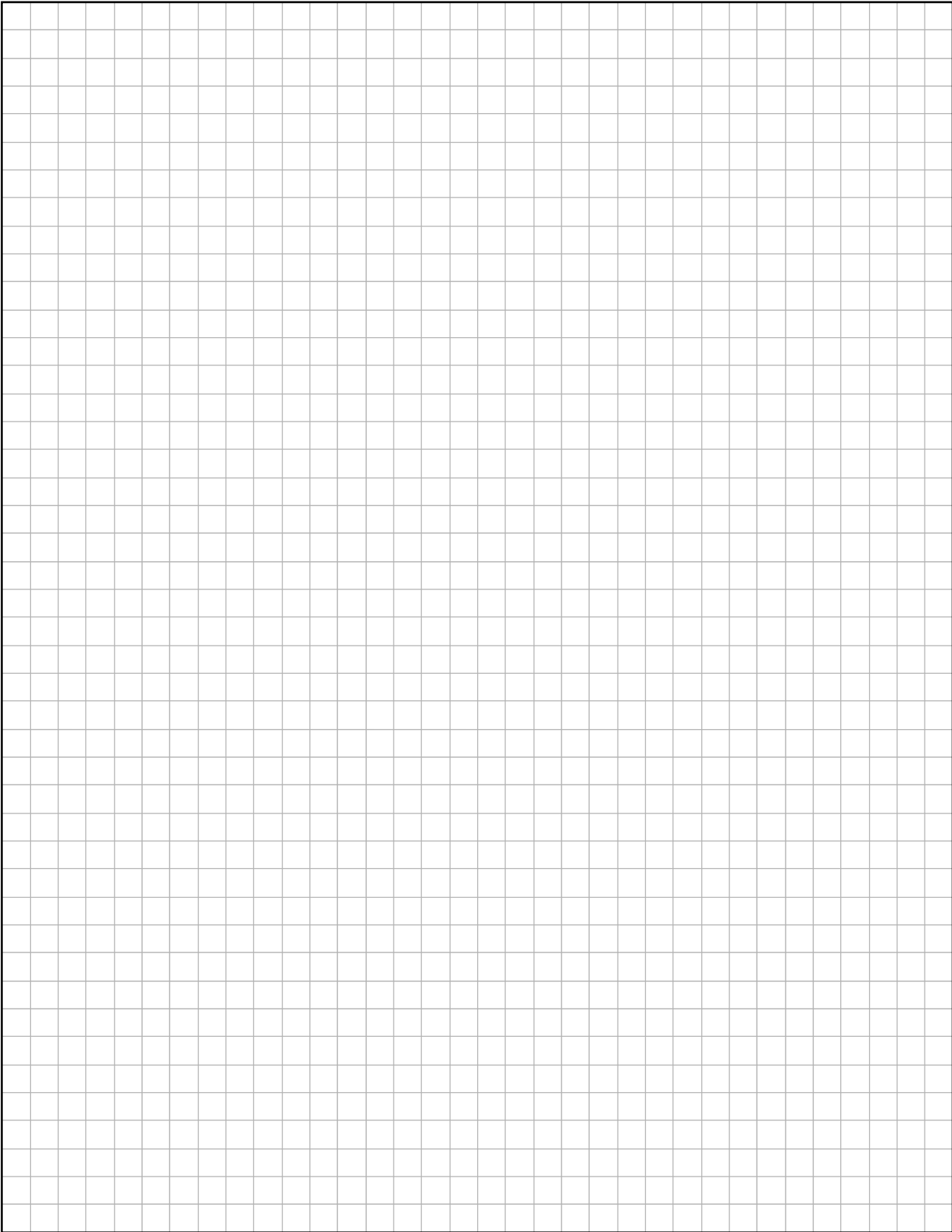
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