## Estimating and Graphing Polynomials LCHL

Using Geogebra, graph the following polynomials and fill in the table below after graphing each one
NOTE: to put indices into an equation use SHIFT and 6 on keyboard to get ^ symbol, then type degree required [e.g for $(x-5)^{2}$ you'd type in ^2]

| Polynomial | Leading coefficient (term with biggest degree/power) positive or negative? | Equation of degree? | Number of roots? | List of roots | Where it crosses $x=$ axis | Where it touches (but doesn't cross) x -axis | End behaviour = Direction of ends/arms (up or down) Both same/different/which up/which down |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})=\mathrm{x}(\mathrm{x}-1)(\mathrm{x}-2)(\mathrm{x}-3)$ |  |  |  |  |  |  |  |
| $\mathrm{f}(\mathrm{x})=\mathrm{x}(\mathrm{x}-2)(\mathrm{x}+5)$ |  |  |  |  |  |  |  |
| $\mathrm{y}=\mathrm{x}(\mathrm{x}+4)(\mathrm{x}-7)(\mathrm{x}-2)(x-5)^{2}$ |  |  |  |  |  |  |  |
| $y=(-x)(x+4)(x-2)(x-5)^{2}$ |  |  |  |  |  |  |  |
| $y=(x)^{2}(x+2)^{3}$ |  |  |  |  |  |  |  |
| $\mathrm{y}=\mathrm{x}^{5}-12 \mathrm{x}^{4}-40 \mathrm{x}^{3}+120 x^{2}$ |  |  |  |  |  |  |  |
| $\mathrm{y}=-\mathrm{x}(\mathrm{x}+3)(x+4)^{3}$ |  |  |  |  |  |  |  |

(Reflection: What examples above have the same characteristics? Is there a pattern to how each graph looks compared to the equation?)

What conclusions can you draw from your graphs and table about the following:

| A polynomial of even degree? |
| :--- |
| A polynomial of odd degree? |
| The leading coefficient is positive? |
| The leading coefficient is negative? |
| Polynomial which has a factor or root which occurs multiple times (known as Multiplicity)? |
| Polynomial which has a factor or root which occurs 2 times? |
| Polynomial which has a factor or root which occurs 3 times? |

