4.2.3 - Forming Equations Given The Roots

4.2 - Algebra - Solving Equations

Leaving Certificate Mathematics

Ordinary Level ONLY

Example 1

Q. Form a quadratic equation from the roots $x = -2, 3$.

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$$(x + 2)(x - 3) \ = \ x(x - 3)$$

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