

## 4.3.3 - Inequalities With Quadratics

### 4.3 - Algebra - Inequalities

Leaving Certificate Mathematics

Higher Level ONLY



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$\therefore 20x^2 - 3x - 2 \geq 0$  for  $x \leq -\frac{1}{4}, x \geq \frac{2}{5}, \quad x \in \mathbb{R}$ .