

4.3.6 - Absolute Value II

4.3 - Algebra - Inequalities

Leaving Certificate Mathematics

Higher Level ONLY



Example 1

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