

4.4.1 - Complex Roots

4.4 - Algebra - Complex Numbers

Leaving Certificate Mathematics

Higher Level ONLY



Example 1

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