(a) The length of the side of a square sheet of cardboard is 12 cm . Find the area of the sheet.

(b) The diagram below shows a square sheet of cardboard of side length 12 cm , from which four small squares, each of side length $h$, have been removed. The sheet can be folded to form an open rectangular box of height $h$.


Write the length and the width of the box in terms of $h$.
$h \mathrm{~cm}$

Length of box $=$ $\qquad$

Width of box $=$ $\qquad$
(c) Show that the volume of the box, in terms of $h$, is $4 h^{3}-48 h^{2}+144 h$.

(d) Find the value of $h$ which gives the maximum volume of the box.

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(e) Find the maximum volume of the box.

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